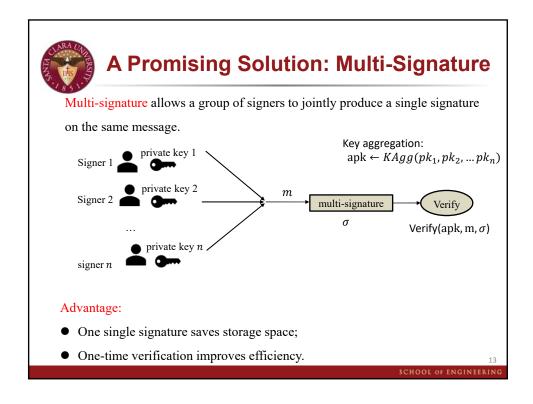




Challenge: Digital Signature Efficiency

- Endorsement process based on digital signature is
 - Inefficient: signature collected from each endorser
 - Resource consuming: verification & storage of multiple signatures;
 significant broadcasting overhead
 - Lack of scalability: 100- 2000 tps.



Bas

Existing Multi-Signature Basis

Basic Scheme	Modulus	Signature length	Computation Operations
RSA	2048 bits	2048 bits	Multiplications
Schnorr	2048 bits	448 bits	Multiplications
BLS	2048 bits	224 bits	Bilinear parings

Multiplication time consuming: 0.0415ms pairing time consuming: 232.7998ms

- Bilinear pairing operation takes much more time than multiplication operation.
- ☐ Considering the signature length and computational cost, we study the Schnorr-based multi-signature schemes.



Schnorr Signatures



$$pk = g^{sk}$$

$$r \leftarrow_R Z_q$$

$$t \leftarrow g^r$$

$$c \leftarrow H(t, m)$$

$$s \leftarrow r + c * sk \mod q$$

$$\sigma \leftarrow (c, s)$$

Verification:

$$c = H(g^s * pk^{-c}, m)$$



"Plain" Schnorr multi-signatures

Signing:



 $r_1 \leftarrow_R Z_q$

 $t_1 \leftarrow g^{r_1}$

 $t \leftarrow t_1 t_2 t_3$

 $c \leftarrow H(t,m)$

 $\sigma \leftarrow (c,s)$



 $pk_2 = g^{sk_2}$

 $r_2 \leftarrow_R Z_q$ $t_2 \leftarrow g^{r_2}$

 $t \leftarrow t_1 t_2 t_3$

 $c \leftarrow H(t,m)$

 $s_1 \leftarrow r_1 + c * sk_1 mod q$ $s_2 \leftarrow r_2 + c * sk_2 mod q$ $s_3 \leftarrow r_3 + c * sk_3 mod q$

 $\sigma \leftarrow (c,s)$

 $s \leftarrow s_1 + s_2 + s_3 \bmod q$ $s \leftarrow s_1 + s_2 + s_3 \bmod q$ $s \leftarrow s_1 + s_2 + s_3 \bmod q$

 $\sigma \leftarrow (c,s)$

 $pk_3=\,g^{sk_3}$

 $r_3 \leftarrow_R Z_q$

 $t_3 \leftarrow g^{r_3}$

 $t \leftarrow t_1 t_2 t_3$

 $c \leftarrow H(t, m)$

Verification:

$$apk \leftarrow pk_1 * pk_2 * pk_3$$
$$c = H(g^s * apk^{-c}, m)$$



Problem 1: Rogue-key Attacks

 a malicious endorser arbitrarily claims his/her public key so that he/she can independently forge a joint signature



$$pk_2 = g^{sk_2}/pk_1$$

$$apk = pk_1 * pk_2 = g^{sk_2}$$

- The malicious endorser can control apk by claiming his/her public key based on the other parties public keys
- o Hence, he/she can compute signatures under apk by him/herself

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Problem 2: k-sum Attacks

• An attack can succeed if a malicious endorser can simultaneously open k-1 signature oracle queries with honest signers on a message m as s_i , where $i \in \{1, ... k-1\}$, and get a valid signature $\sigma \leftarrow (c^*, s^*)$ on a target message $m^* \neq m$, meaning that

$$c^* = \sum_{i=1}^{k-1} c_i \qquad s^* = \sum_{i=1}^{k-1} s_i + c^* * sk \qquad \qquad c^* = H(g^s * apk^{-c}, m^*)$$

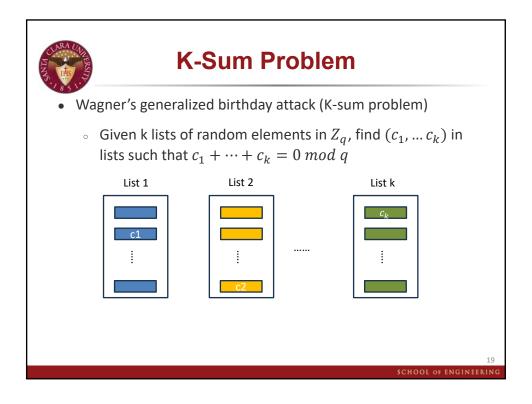
$$= H(g^{\sum_{i=1}^{k-1} r_i}, m^*)$$

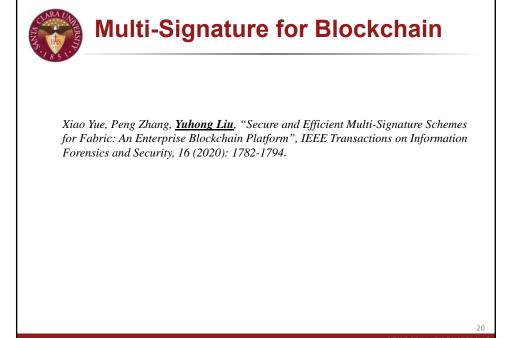
• Since $c_i \leftarrow H(t_i, m)$, where t_i can be controlled by the attacker, an attack can succeed if the attacker is able to construct

$$c^* = \sum_{i=1}^{k-1} c_i = \sum_{i=1}^{k-1} H(t_i, m) \qquad \sum_{i=1}^{k-1} H(t_i) m = H(g^{\sum_{i=1}^{k-1} r_i} [m])$$

• The last signer of the endorsement, with excessive power, can forge a joint signature on a new message.

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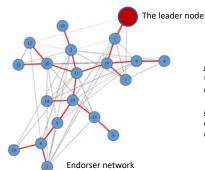






CoSi: Multi-signature Scheme

- A very popular Schnorr-based scheme
- High scalability due to the spanning tree structure
 - a loop-free logical topology
 - o a single active path between any two network nodes.



<u>K-sum problem attacks</u>: the leader of the endorsement, with excessive power, can forge a joint signature on a new message.

<u>Roque-key attacks</u>: a malicious endorser arbitrarily claims his/her public key so that he/she can independently forge a joint signature

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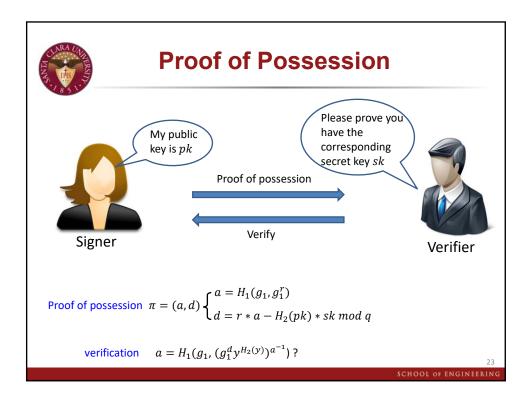
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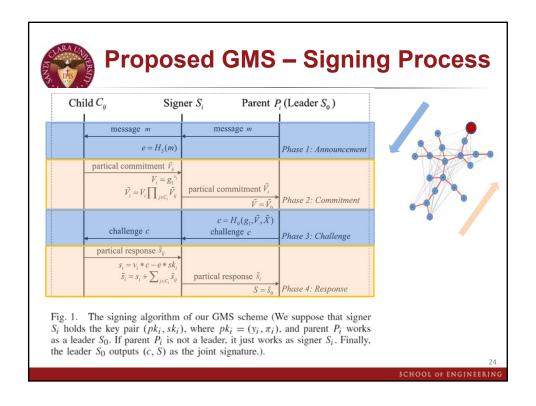


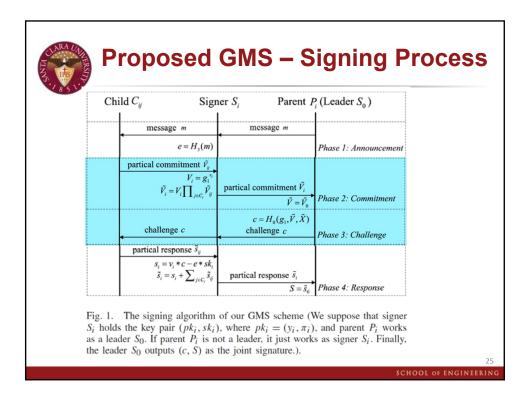
Proposed Schemes

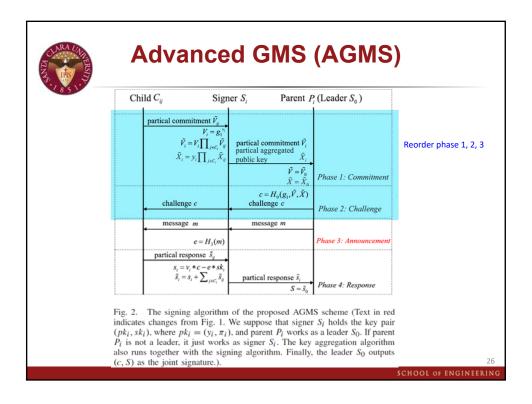
- A Gamma Multi-Signature (GMS) security
- Spanning tree structure (high scalability)
 - Proof of possession against rogue-key attacks
 - Improved signing process against k-sum attacks
- An Advanced Gamma Multi-Signature (AGMS) efficiency
 - Improved online efficiency by reordering the signing process

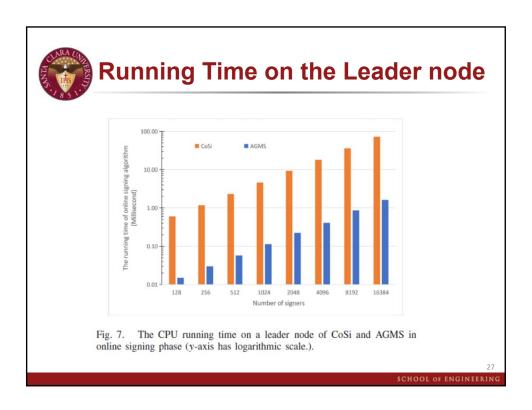
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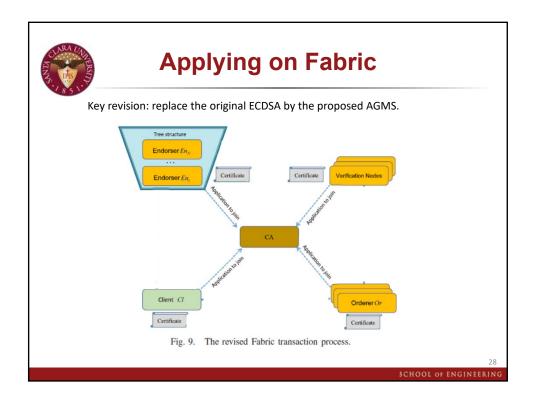


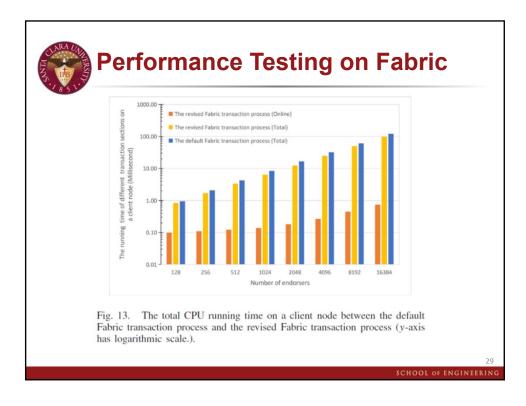














Another Problem – Flexible Endorsement

■ Endorsement policy in Fabric can be expressed as:

EXPR(E[, E...]),

where *EXPR* is "AND", "OR" or "OutOf"; and E is either an endorser or another nested call to EXPR.

■ Typical endorsement policies are monotonic and group-based:

AND('Org1.member',' Org2.member', ...),

where "*OR*" expression is used to check if any member from Org1 (and Org2) has endorsed.

■ Not supported by existing Multi-signature schemes: Existing multi-signature schemes mainly focus on "AND" relationship among multiple singers, they can only support individual-based endorsement policies like "AND('member1','member2',...)".



Peng Zhang, Yongwen Huang, Fa Ge, <u>Yuhong Liu</u>, "Group-Oriented Multi-Signature Supporting Monotonic Endorse Policies in Hyperledger Fabric", IEEE Blockchain 2023, Hainan, China, Dec. 17-23, 2023

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The Proposed Scheme

- We propose a Group-oriented Multi-Signature scheme, which supports secure and more flexible endorsement policy
- Based on the proposed scheme, the transaction protocol in Fabric is optimized, so that the block size and verification time are reduced.

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The Proposed Scheme

Group-oriented multi-signature scheme with smart contract

- ☐ Smart contract on blockchains is distributed on peer-to-peer networks, publicly verifiable, and executed automatically.
- By introducing public and trustworthy smart contracts to be the last signer responsible for commitment operations, *k*-sum problem attacks are prevented.

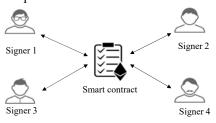


Fig. 3 The network structure of our scheme

It is responsible for:

- 1. Collecting commitments $R_{i,j}$ from all signers;
- 2. Recording the timestamp t and computing the last commitment $W = g^{H(t)}$;
- Computing and Distributing the joint commitments.

$$R = W^{\theta} \prod_{i=1}^{\theta} R_{i,j}$$

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The Proposed Scheme

■ By introducing Chinese Remainder Theorem to combine all public keys of members in a group into one group public key, the public key of each member is unknown to all others except the group administrator, so that only the group public key is involved in verification.

$$\begin{cases} k_i = X_{i,1} \pmod{p_{i,1}} \\ \vdots \\ k_i = X_{i,\eta} \pmod{p_{i,\eta}} \end{cases}$$

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Security Analysis

We conduct a security analysis on the proposed scheme. Based on the difficulty problem assumption, our scheme satisfies the unforgeability, anonymity, revocability and traceability.

- ☐ Unforgeability: The signature cannot be forged by an attacker.
- ☐ Anonymity: The identity of the signer will not be revealed.
- Revocability: Signers who exit the group cannot be regenerated into legal signatures.
- ☐ Traceability: Only the group administrator knows the identities of the members participating in the multi-signature.

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Comparison

Table 1 The comparisons of key and signature length (θ represents the number of groups)

Scheme	Public key	Private key	Signature
Musig2	G	$ \mathbb{Z}_{\alpha} $	$ \mathbb{G} + \mathbb{Z}_{\alpha} $
GMS	G	$ \mathbb{Z}_{\alpha} $	$ \mathbb{G} + (\theta + 1) \mathbb{Z}_{\alpha} $

Table 2 The comparisons of computational cost and security assumptions (Exp represents the calculation cost of an exponential operation in the group)

Scheme	Sign	Verify	Join	Revoke	Assumptions
Musig2	7EXP	2EXP	-	-	AOMDL
GMS	2EXP	2EXP	1EXP	0EXP	DL

