

Los Alamos Northern New Mexico section (LANNM)

Computer Science Chapter of IEEE

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Unified Lattice Boltzmann Computation for Patient-specific Hemodynamics in Healthy and Diseased Aorta

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Contributors

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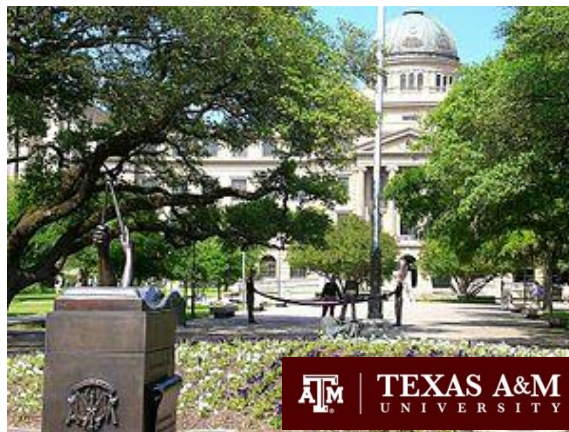
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IU Medicine: Shawn D. Teague





B.S., Physics

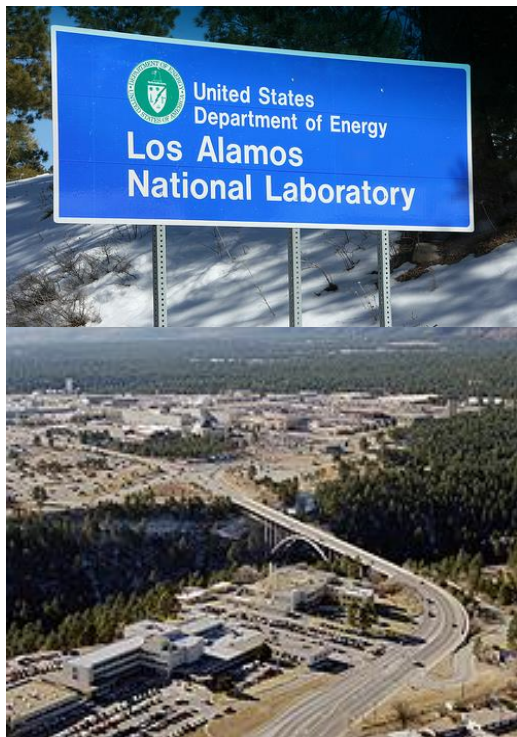


Ph D, Aerospace Engineering



Ph D, Physics

Postdoc



Postdoc



Assistant Professor

Previous Research Experience

● **Turbulence computation (modeling and simulation)**

Kinetic CFD, lattice Boltzmann method

- Decaying isotropic turbulence w/wo rotation — Texas A&M
- Turbulent rectangular jets — Texas A&M
- Flaming in reacting flow — Texas A&M
- Heat/mass transfer in natural convection — Los Alamos
- Binary scalar mixing with equal and unequal masses — Texas A&M
- Peristaltic transport in gastrointestinal tract — Penn State

Hydrodynamic CFD, Navier-Stokes equations

- Compressible Rayleigh-Taylor instability w/wo combustion, massive parallel — Los Alamos

● **Applied fluid mechanics**

- Linear stability analysis of compressible RT instability in cylindrical geometry — Los Alamos
- Rapid distortion theory in compressible turbulence — Texas A&M
- Public turbulence database enabled analysis for Lagrangian turbulence — Johns Hopkins

● **Cyber CFD and database technology (computational and experimental data)**

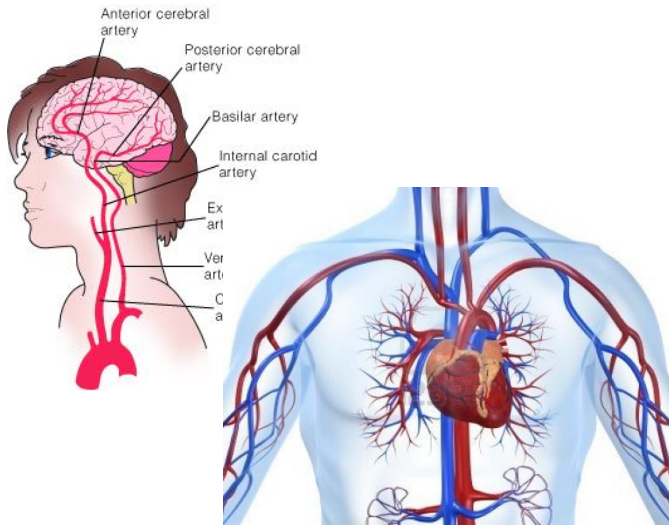
- Web-accessed turbulence database, “cyber fluid dynamics” — Johns Hopkins
- Cohesive experimental database for predicting long-term corrosion/erosion of steel exposed to flowing liquid lead/lead bismuth eutectic — Los Alamos

Outline

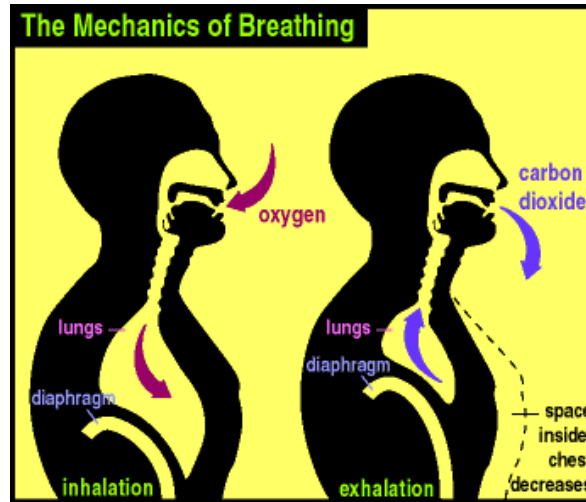
- Background and research motivation
- Unified computation platform for patient-specific computational hemodynamics using lattice Boltzmann method
- Preliminary results on patient-specific hemodynamics in healthy and diseased aorta
- Summary

Flows in Human Body

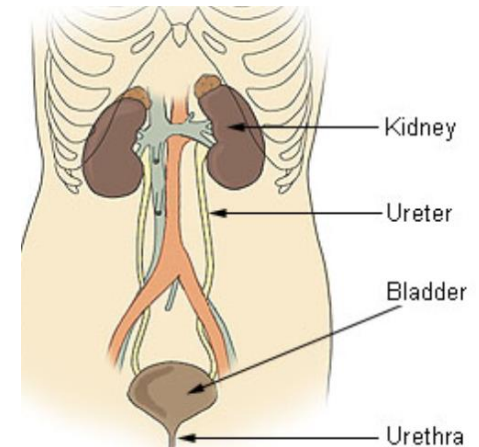
Circulatory System



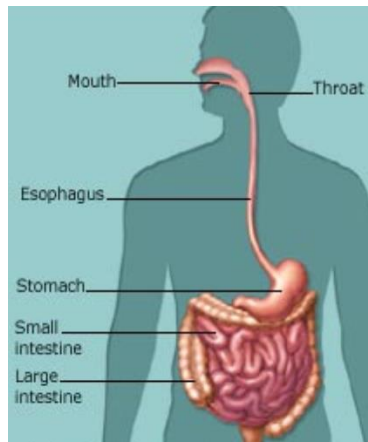
Respiratory System



Urinary System



Digestive System



Fluid-structure interaction

Structure:

- Arbitrary geometry
- Bifurcations
- Deformable
- Willfully/compliantly moving

Fluid/flow:

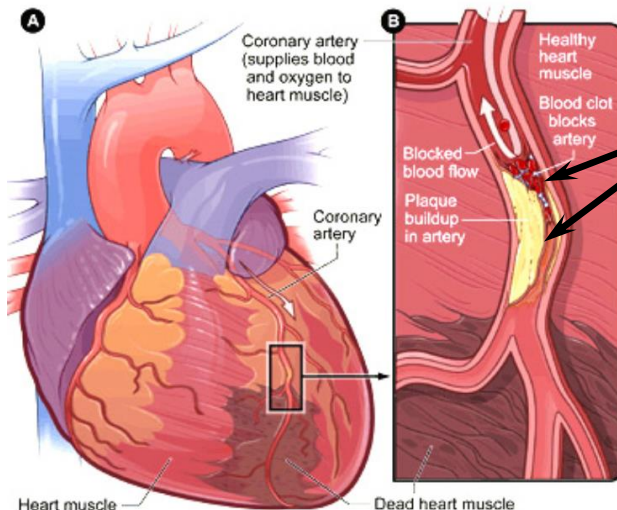
- Pulsatile
- Laminar/turbulence
- Non-Newtonian
- Multiphase

Cardiovascular Disease Facts

from www.CDC.gov

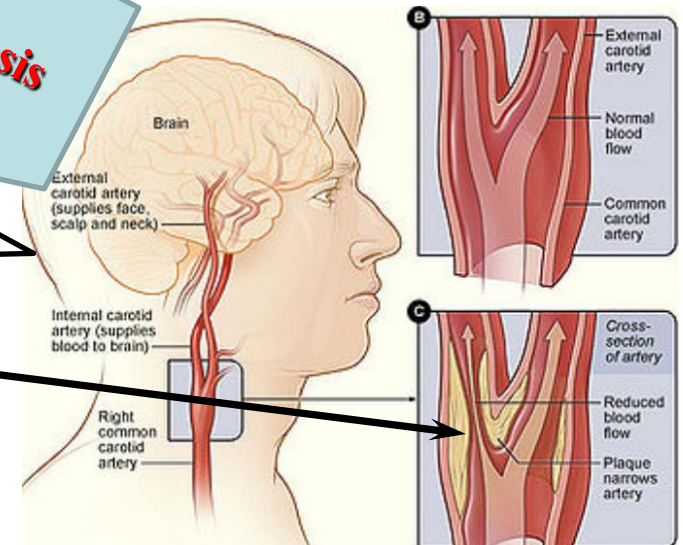
Heart Attack

- Killing **600K** people, **1 in every 4 deaths**
- One** heart attack every **34 seconds**
- \$108.9 billion** for coronary heart disease



Blockage

Atherosclerosis



Stroke

- Killing **130K** people, **1 in every 19 deaths**
- One** heart attack every **34 seconds**
- \$38.6 billion** for health care, medication, lost productivity

Hypothesis: hemodynamics likely reveals the mechanism of plaque disruption or embolization

Hemodynamics: In Vivo Imaging

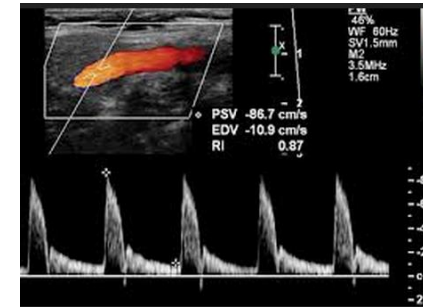
Phase-Contrast Magnetic Resonance Imaging

J Thorac Imaging • Volume 28, Number 4, July 2013

REVIEW ARTICLE

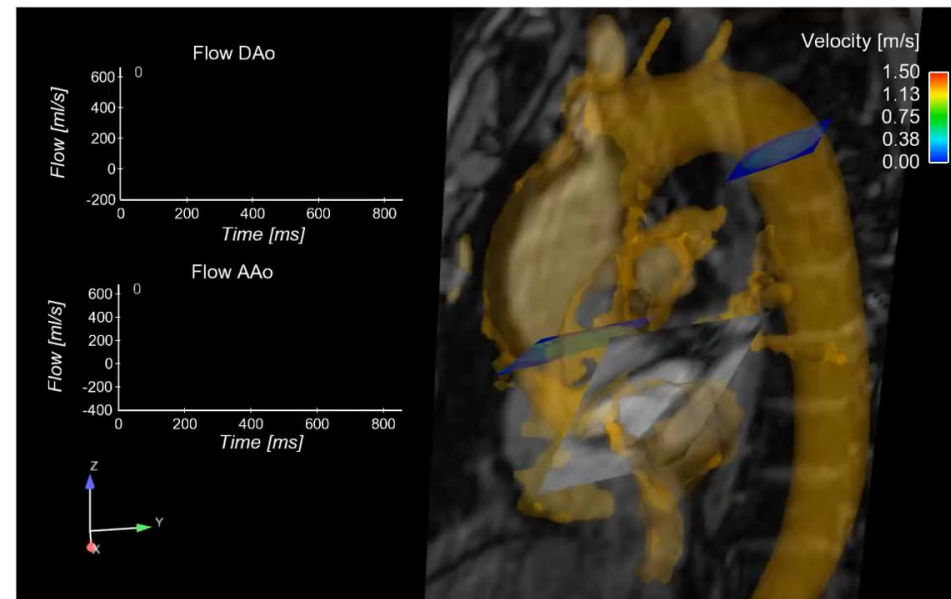
Cardiothoracic Magnetic Resonance Flow Imaging

Michael D. Hope, MD, Tony Sedlic, MD,* and Petter Dyverfeldt, PhD*†‡*

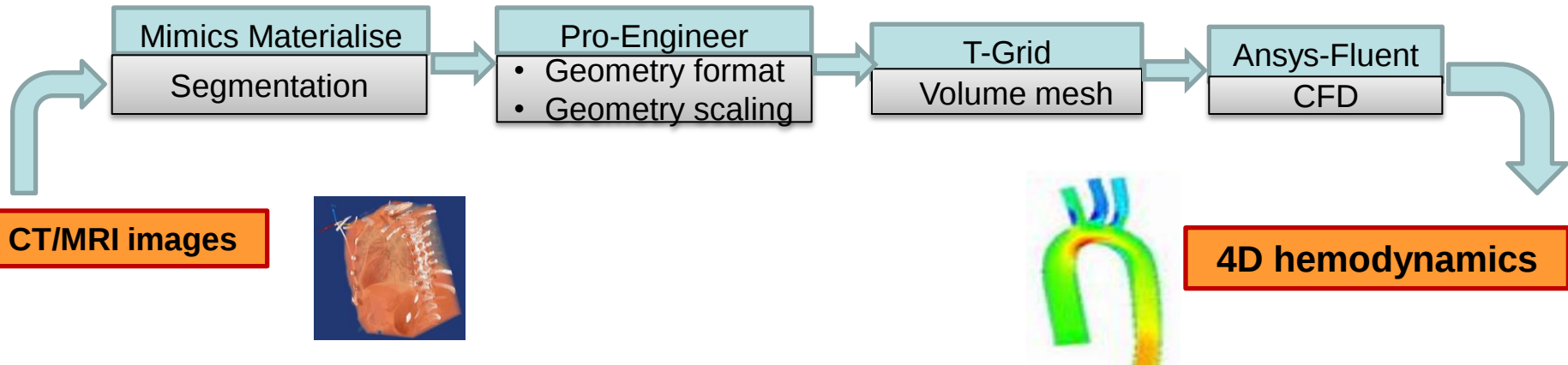


Challenges for clinical application

- Long scan time (hours)
- Data processing
(time consuming,
specific operator skills)
- Lack of proven clinical applications
- Limited to heart and great vessels

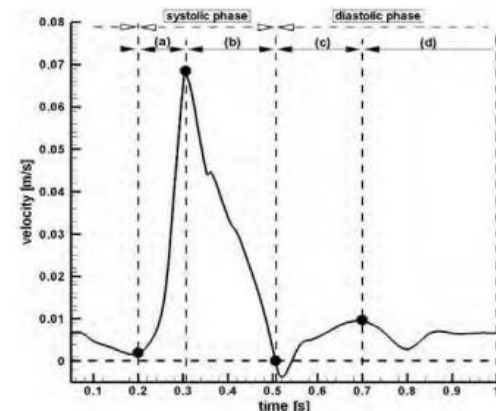


Patient-specific Computational Fluid Dynamics

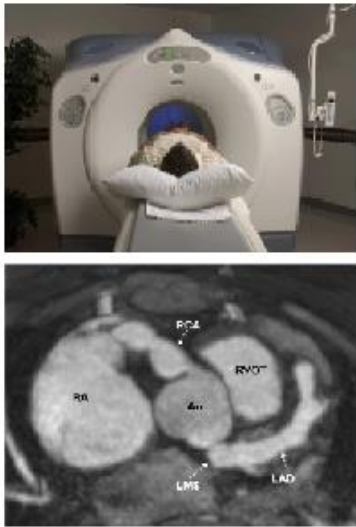


Limitations:

1. Inadequate for pulsatile flow
2. Modeling — FSI, Multiphase, etc.
3. GPU parallel computing



Unified Computation Platform



Integration

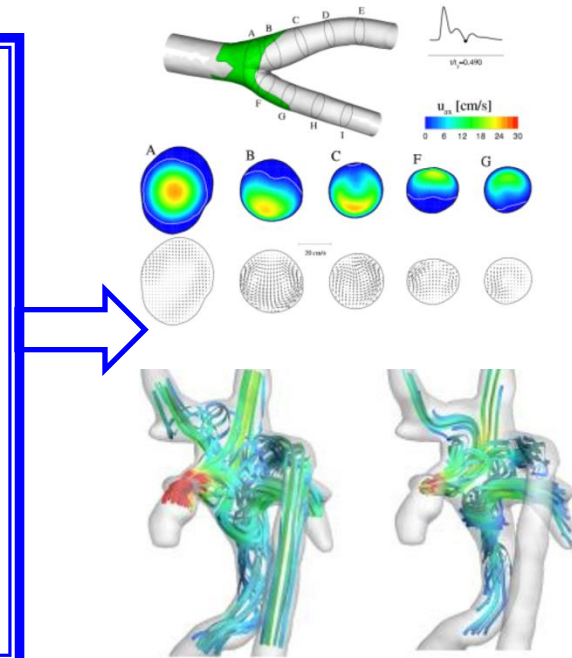
Segmentation — CT/MRI

Fluid-structure Interaction

Turbulence — pulsatile flow

Multiphase — non-Newtonian

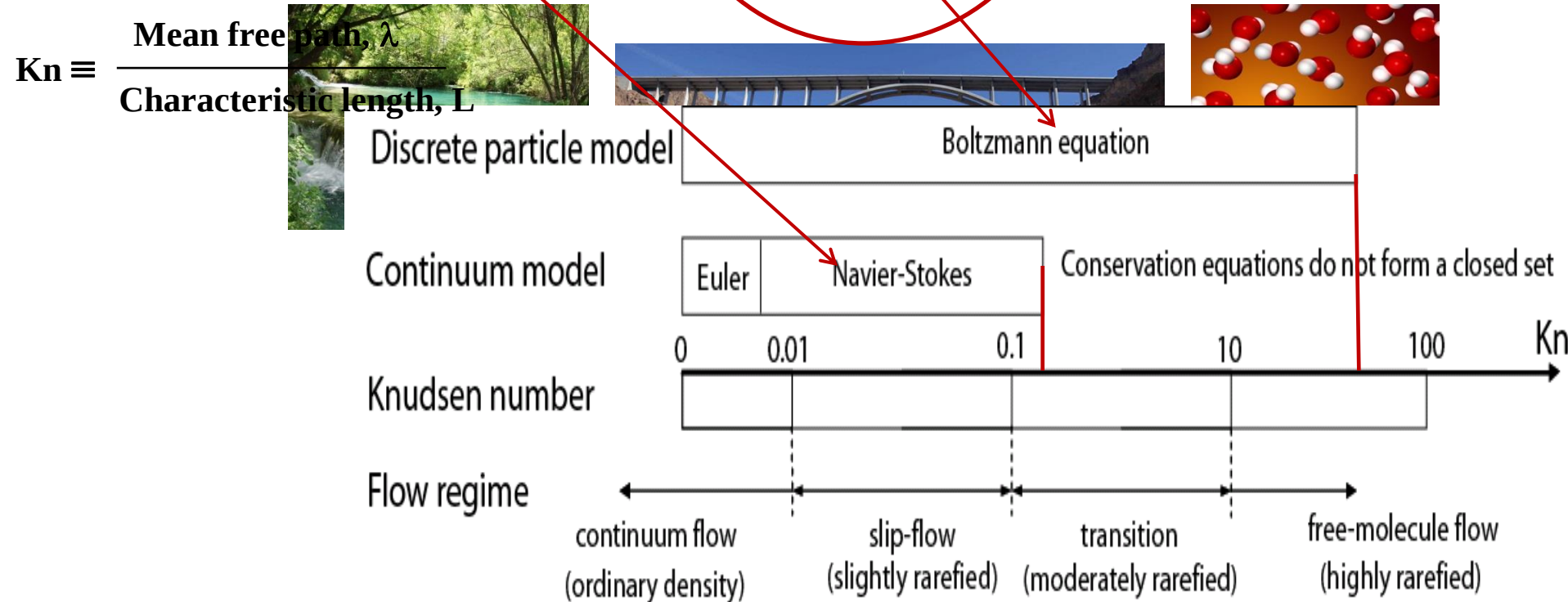
Parallelism — GPU



Lattice Boltzmann Method

Descriptions of Fluid Dynamics

	Macroscopic	Mesoscopic	Microscopic
Theory	Hydrodynamics	Kinetic Theory	Molecular Dynamics
Equations	Navier-Stokes	Boltzmann	Newton-Hamilton
subject	Continuum variables	Particle distribution function	Particle trajectories



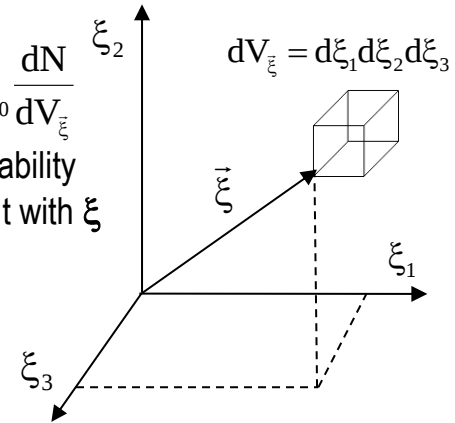
The diagram is adapted from Anderson J., *Hypersonic and high temperature gas dynamics*, McGraw-Hill, 1989.

Boltzmann Equation

Key variable: particle distribution function

$$f(\vec{x}, \vec{\xi}, t) = \frac{\rho}{N} \lim_{dV_{\vec{\xi}} \rightarrow 0} \frac{dN}{dV_{\vec{\xi}}}$$

density weighted probability
to find a particle at $\vec{x}$, t with $\vec{\xi}$



Molecular phase space

$$\frac{\partial f}{\partial t} + \vec{\xi} \cdot \nabla f + \frac{\partial f}{\partial \vec{\xi}} \cdot \vec{F} = J(f)$$

collision operator

$$\int \begin{bmatrix} 1 \\ \vec{\xi} \\ (\vec{\xi} - \vec{u})^2 \end{bmatrix} J(f) d\vec{\xi} = \begin{bmatrix} 0 \\ 0 \\ 0 \end{bmatrix}$$

Collision satisfies conservation laws

$$\frac{\partial \rho}{\partial t} + \frac{\partial (\rho u_i)}{\partial x_i} = 0$$

$$\rho \left(\frac{\partial u_i}{\partial t} + u_j \frac{\partial u_i}{\partial x_j} \right) + \frac{\partial P_{ij}}{\partial x_i} = \rho f_i$$

$$\rho \left(\frac{\partial e}{\partial t} + u_j \frac{\partial e}{\partial x_j} \right) + \frac{P_{ij} \partial u_i}{\partial x_j} + \frac{\partial q_i}{\partial x_i} = 0$$

P_{ij} , and q_i closures

Hydrodynamic variables

Density

$$\rho(\vec{x}, t) = \int f(\vec{x}, \vec{\xi}, t) d\vec{\xi}$$

Momentum

$$\rho \vec{u}(\vec{x}, t) = \int \vec{\xi} f(\vec{x}, \vec{\xi}, t) d\vec{\xi}$$

Internal Energy

$$\rho e(\vec{x}, t) = (1/2) \int \vec{c}^2 f(\vec{x}, \vec{\xi}, t) d\vec{\xi}$$

Stress tensor

$$P_{ij}(\vec{x}, t) = - \int c_i c_j f(\vec{x}, \vec{\xi}, t) d\vec{\xi}$$

Heat flux density

$$\vec{q}(\vec{x}, t) = (1/2) \int \vec{c} (\vec{c} \cdot \vec{c}) f(\vec{x}, \vec{\xi}, t) d\vec{\xi}$$

$$\vec{c} \equiv \vec{\xi} - \vec{u}$$

.....

Non-hydrodynamic moments

Remarks:

Bhatnagar-Gross-Krook (BGK) approximation

1. BE covers NS, and more than NS

2. Once f known, hydrodynamics known

$$\frac{\partial f}{\partial t} + \vec{\xi} \cdot \nabla f + \frac{\partial f}{\partial \vec{\xi}} \cdot \vec{F} = -Z(f - f_M)$$

Z : Average collision frequency

f_M : Maxwell-Boltzmann equilibrium distribution function

Higher order moments

Beyond NS

N-S
Equations

A Passage from BGKBE to BGKLE

BGK or SRT model

X. He and L-S Luo, PRE 56, 6811(1997)

$$\partial f / \partial t + \vec{\xi} \cdot \nabla f = -Z(f - f_M), \quad f = f(\vec{x}, \vec{\xi}, t)$$

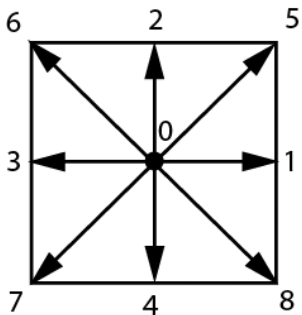
1. Discretization of time

$$f(\vec{x} + \vec{\xi} \delta t, \vec{\xi}, t + \delta t) = f(\vec{x}, \vec{\xi}, t) - [f(\vec{x}, \vec{\xi}, t) - f_M(\vec{x}, \vec{\xi}, t)] / \tau$$

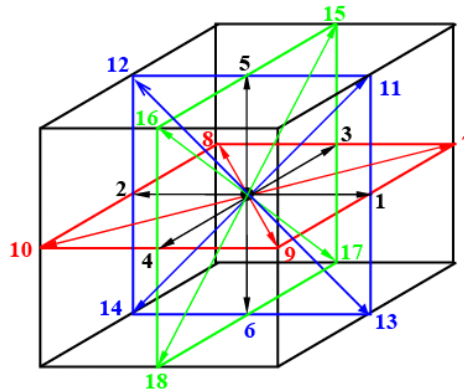
$\tau = 1/(Z\delta t)$

2. Discretization of physical space and molecular velocity space coherently in finite directions satisfying conservation laws and symmetry needs

3. Taylor expand f_M at low Mach number limit and determine coefficients based on conservation laws and symmetry needs



$$\vec{e}_\alpha = \begin{cases} (0,0) & \alpha=0 \\ (\pm 1,0), (0,\pm 1) & \alpha=1-4 \\ (\pm 1,\pm 1) & \alpha=5-8 \end{cases}$$



$$\vec{e}_\alpha = \begin{cases} (0,0) & \alpha=0 \\ (\pm 1,0,0), (0,\pm 1,0), (0,0,\pm 1) & \alpha=1-6 \\ (\pm 1,\pm 1,0), (\pm 1,0,\pm 1), (0,\pm 1,\pm 1) & \alpha=7-18 \end{cases}$$

$$f_\alpha(\vec{x} + \vec{e}_\alpha \delta t, t + \delta t) = f_\alpha(\vec{x}, t) - [f_\alpha(\vec{x}, t) - f_\alpha^{(eq)}(\vec{x}, t)] / \tau$$

Chapmann-Enskog technique

$$\nabla \cdot \vec{u} = 0, \quad \partial \vec{u} / \partial t + \vec{u} \cdot \nabla \vec{u} = -\nabla p / \rho + \nu \nabla^2 \vec{u}$$

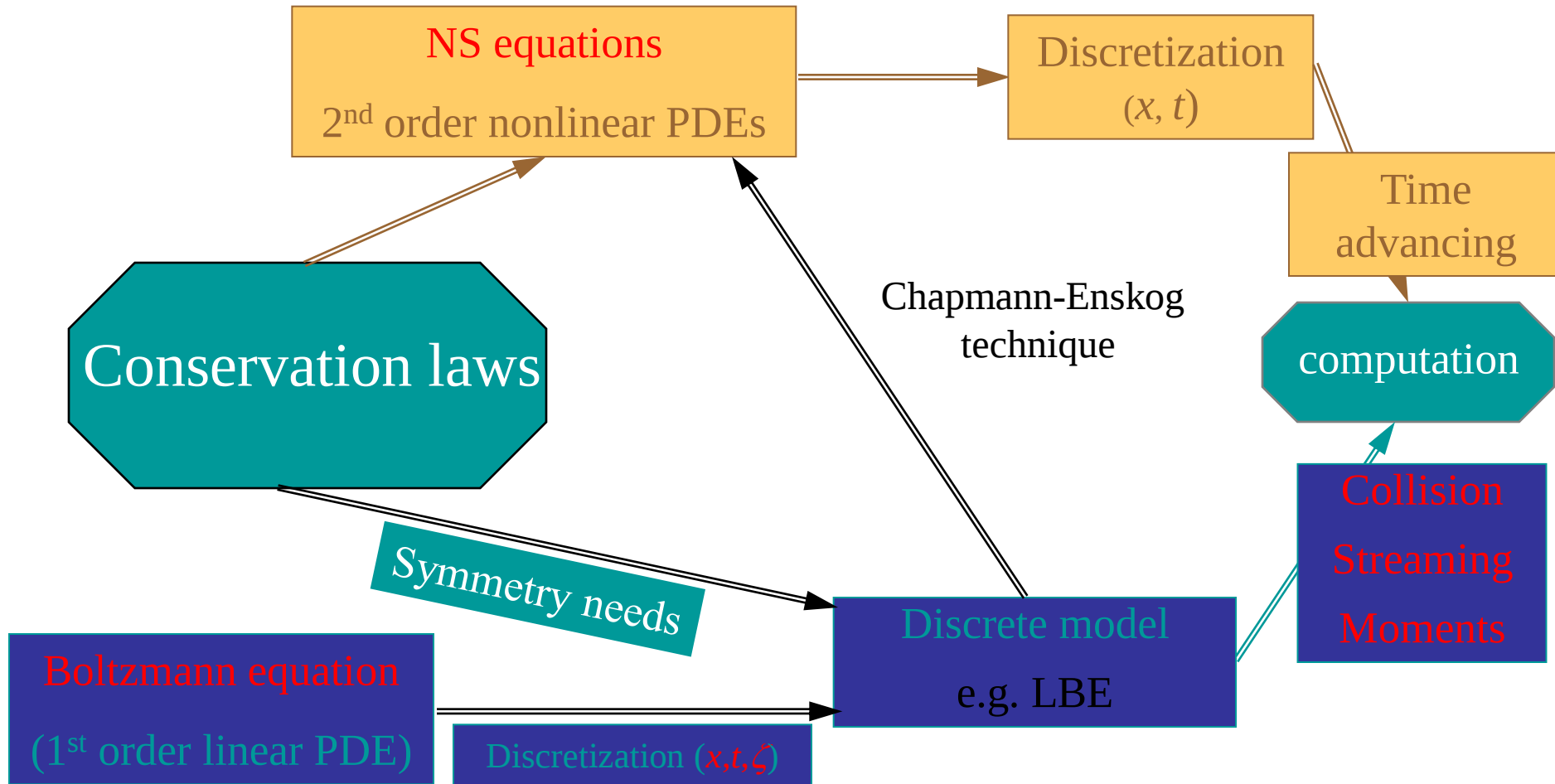
$$\tau = 3\nu / (c\delta x) + 0.5$$

$$\rho = \sum f_\alpha$$

$$\rho \vec{u} = \sum c \vec{e}_\alpha f_\alpha$$

Computation Methodologies

Computational Fluid Dynamics (CFD)



Digital Fluid Dynamics (DFD)

Potential Advantages of LBM

$$f_{\alpha}(\vec{x} + \vec{e}_{\alpha} \delta t, t + \delta t) = f_{\alpha}(\vec{x}, t) - [f_{\alpha}(\vec{x}, t) - f_{\alpha}^{(eq)}(\vec{x}, t)] / \tau$$

$$\rho = \sum f_{\alpha}, \rho \vec{u} = \sum \vec{e}_{\alpha} f_{\alpha}$$

● Simpler implementation

Linear equation
Discrete equation
Single variable
Arithmetic calculation
(no derivative involved)

● More physical concepts: collision and streaming

e.g. Single phase: self collision
Multiphase: self and mutual collisions
Miscible: attracting
Immiscible: repelling
No-slip boundary: bounce-back

- Easy handling of **complicated geometry or boundary**
e.g. porous media, bio-transport, etc.
- Ideally suited for **multi-phase** flows
e.g. interfacial dynamics, fluid structure interaction, etc
- Good candidate for problems **beyond Navier-Stokes**,
e.g. rarified gas, plasma, micro/nano fluidics
- Well suited for large-scale, **parallel** (GPU) computing

A Historic View of LBM

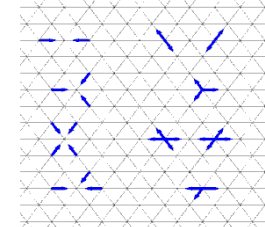
Lattice gas automata (LGA)

Frisch, Hasslacher, and Pomeau, PRE, 1986

$n_\alpha(\mathbf{x} + \delta_t \mathbf{e}_\alpha, t + \delta_t) = n_\alpha(\mathbf{x}, t) + C_\alpha(\{n_\beta\})$, $C_\alpha(\{n_\beta\})$: collision operator

Main drawbacks: $n_\alpha \in [0,1]$: Boolean particle number

Intrinsically noisy; lack of Galilean invariance,
unphysical pressure; unphysical conserved quantities



Discrete molecular phase space

Ensemble Average of LGA: $f_\alpha = \langle n_\alpha \rangle \in [0,1]$, G. McNamara and G. Zanetti, PRE, 1988

Lattice Boltzmann method (LBM)

Qian, d'Humières, Lallemand, Europhys. Lett. (1992), H Chen, S Chen, and Matthaeus, Phys. Rev. E, 1992,

$f_\alpha(\mathbf{x} + \delta_t \mathbf{e}_\alpha, t + \delta_t) = f_\alpha(\mathbf{x}, t) + \Omega_\alpha(\mathbf{x}, t)^*$

f_α : particle number with $\mathbf{e}_\alpha$ at $\mathbf{x}$

Ω_α : collision operator

* Empirical evolution of LGA historically. Mathematical proof by Abe, JCP(1997), He&Luo, PRE (1997)

Restrictions: — incompressible flow

Small Mach number assumption; Small knudsen number assumption;
thermal model numerically unstable; not clear how to extend beyond NS

Bhatnagar-Gross-Krook approximation

$\Omega_\alpha(\mathbf{x}, t) = -[f_\alpha(\mathbf{x}, t) - f_\alpha^{(eq)}(\mathbf{x}, t)]/\tau$

Moment expansion, Shan & He, PRL, 1998

Kinetic theory representation of hydrodynamic Navier-Stokes and beyond

Shan, Yuan, and Chen, JFM, 2006

Breakthroughs:

Compressible, shocks, rarified, thermodynamic effect

LBM for Image Processing

Image segmentation

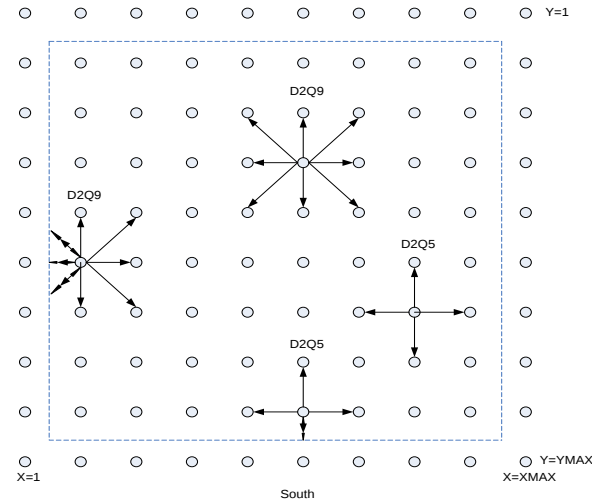
Image denoising

Image Filtering

Image lighting

- Zhao, Y., *Lattice Boltzmann based PDE solver on the GPU*. Visual Computer, 2008.
- Zhao, Y. *GPU-Accelerated Surface **Denoising and Morphing** with Lattice Boltzmann Scheme*, in *IEEE International Conference on Shape Modeling and Applications*, 2008.
- Hagan, A. and Zhao, Y., *Parallel 3D **Image Segmentation** of Large Data Sets on a GPU Cluster*, in the *5th International Symposium on Visual Computing*, 2009.
- Cahang, Q. and Yang, T., *A lattice Boltzmann method for **image denoising***. IEEE Transactions on Image Processing, 2009.
- Zhang, W. and Shi, B., *Application of Lattice Boltzmann Method to **Image Filtering***. Journal of Mathematical Imaging and Vision, 2012.
- Balla-Arabé, O. and Gao, X., *A fast and robust level set method for **image segmentation** using fuzzy clustering and lattice Boltzmann method*. IEEE Trans Syst Man Cybern B., 2012.

Modern Graphics and Visualization



- Modern images are digitized.
- PDEs are widely used in graphics and visualization applications
 - Image processing
 - Surface processing
 - Volume graphics and visualization

Image Segmentation

Caselles, Kimmel, and Sapiro, Int. J. Comp. Vision, 1997.

Geometric Active Contour (GAC) model:

$$\frac{\partial \vec{C}}{\partial t} = [g(\kappa + \alpha) - (\nabla g \cdot \vec{N})] \vec{N}$$

inward normal

I_0 : original image

C : evolving curve

κ : curvature

g : edge-stopping function

σ : smooth parameter

Image

smoothing

$$g = \frac{1}{1 + |\nabla(G_\sigma * I_0)|^2}$$

gradient of a Gaussian smoothed data

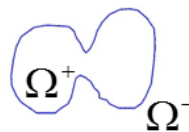


Level set formulation — diffusion equation with an external force

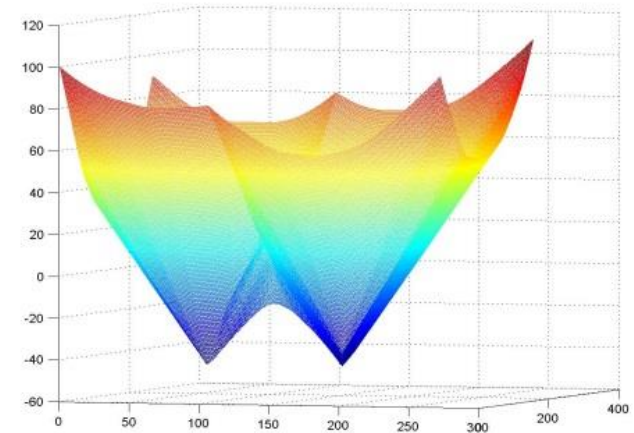
$$\frac{\partial u}{\partial t} = \nabla \cdot (g \nabla u) + F$$

u : level set function — distance field of the active contour

F : $g\alpha$



Contour (zero level set)

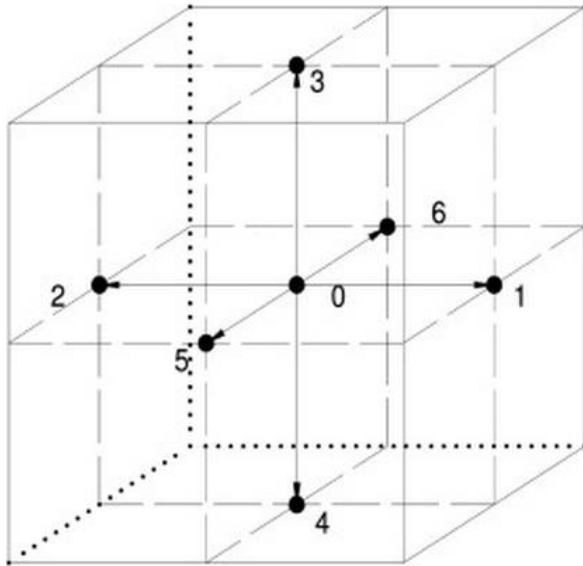


LB-GAC Model

$$f_i(\vec{x} + \Delta t \cdot \vec{e}_i, t + \Delta t) - f_i(\vec{x}, t) = \omega \cdot [f_i^{\text{eq}}(\vec{x}, t) - f_i(\vec{x}, t)] + \Delta t F_i$$

($i = 1, \dots, 7$)

D3Q7 lattice



$$\omega = 2/(1 + 6\Delta t g)$$

$$F_i(\vec{x}, t) = \frac{1}{7} F(\vec{x}, t)$$

$$f_i^{\text{eq}}(\vec{x}, t) = \frac{1}{7} u(\vec{x}, t)$$

$$u(\vec{x}, t) = \sum_{i=1}^7 f_i(\vec{x}, t)$$

I. Ginzburg, Equilibrium-type and Link-type Lattice Boltzmann models for generic advection and anisotropic-dispersion equation, Adv Water Resour, 2005

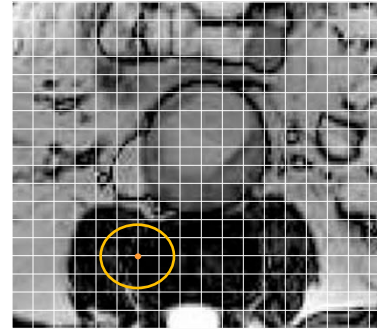
Segmentation Flow Chart

Given image data $I_0(\vec{x}) \Rightarrow g(\vec{x})$

$$F_i(\vec{x}, 0) = \alpha g(\vec{x}, 0) / 7$$

Initialization $u(\vec{x}, t) \begin{cases} < 0, \text{inside} \\ > 0, \text{outside} \\ = 0, \text{int erface} \end{cases}$

$$f_i(\vec{x}, 0) = f_i^{\text{eq}}(\vec{x}, 0) = u(\vec{x}, 0) / 7$$



LBM collision

$$f'_i(\vec{x}, t) = f_i(\vec{x}, t) + \omega \cdot [f_i^{\text{eq}}(\vec{x}, t) - f_i(\vec{x}, t)] + \Delta t F_i$$

streaming

$$f_i(\vec{x} + \Delta t \cdot \vec{e}_i, t + \Delta t) = f'_i(\vec{x}, t)$$

Updated distance function

$$u(\vec{x}, t + \Delta t) = \sum_i f_i(\vec{x}, t + \Delta t)$$

Update $u(\vec{x}, t + \Delta t) = 0$

$$f_i^{\text{eq}}(\vec{x}, t + \Delta t) = u(\vec{x}, t + \Delta t) / 7$$

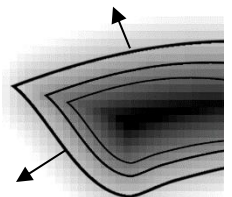
Solid volume

Voxelise a 3D triangular-polygon mesh to compute the volume of boundary cell

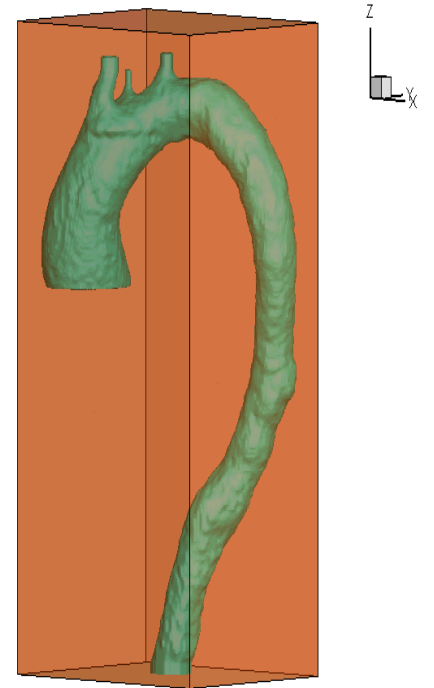
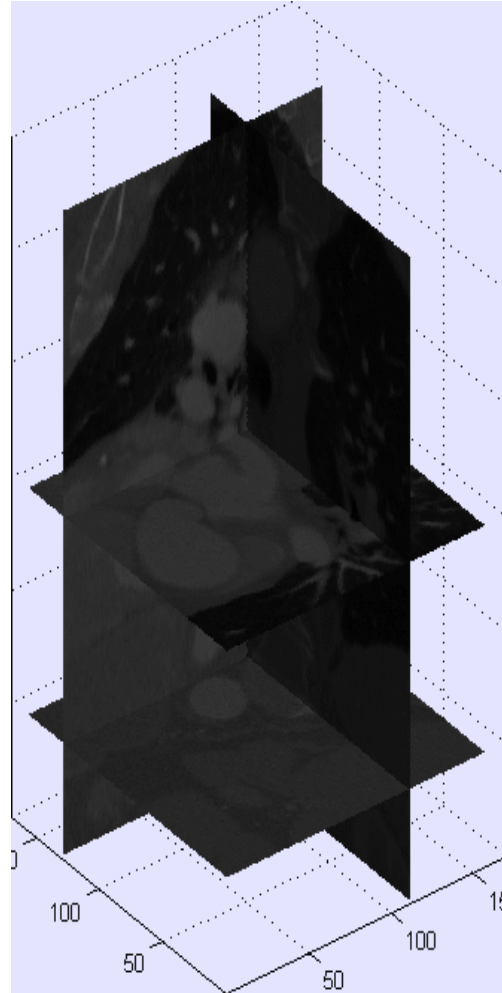
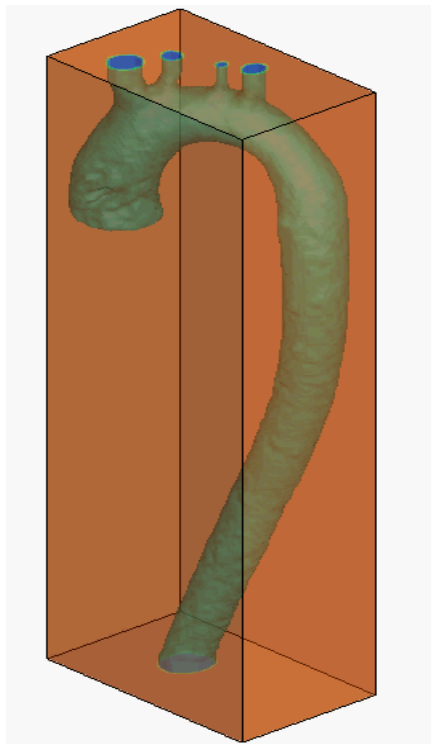
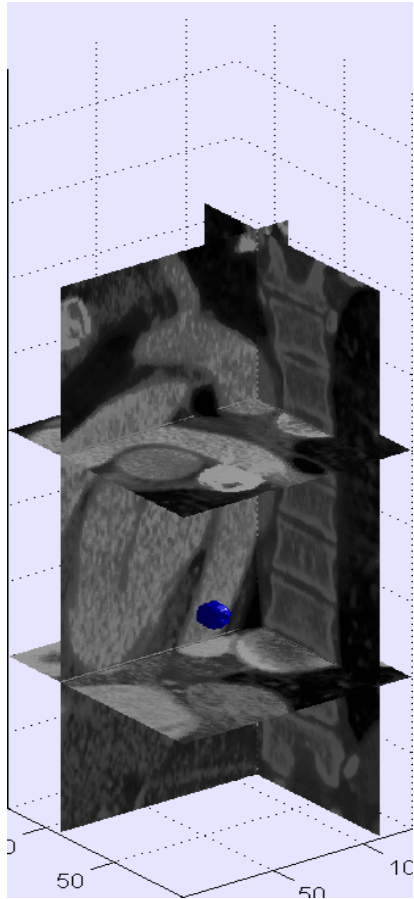
$$0 < p(\vec{x}) = V_s / V < 1$$

Wall normal direction

$$\vec{N} = \frac{\nabla u}{|\nabla u|}$$



Healthy and Diseased Aortas from CT Images



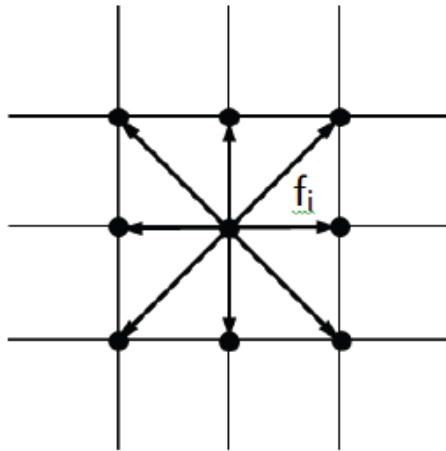
Mass-conserved Volumetric LBM

Node-based LBM

Time evolution of particle distribution functions

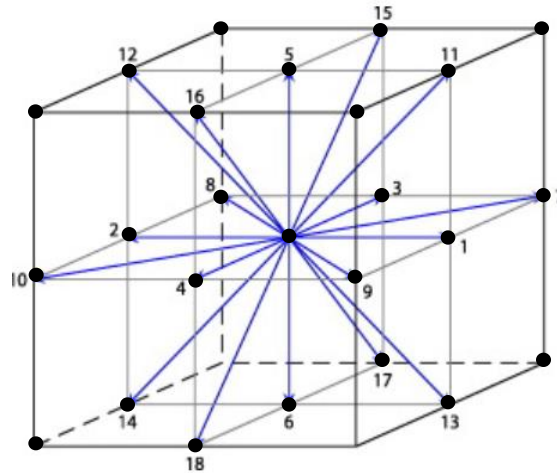
$$f_{\alpha}(\vec{x} + \vec{e}_{\alpha}\Delta t, t + \Delta t) = f_{\alpha}(\vec{x}, t) + \Omega_{\alpha}(\vec{x}, t)$$

$\alpha=0,1,\dots,8$



D2Q9

$\alpha=0,1,\dots,18$



D3Q19

Node-based LBM for Curved Boundary

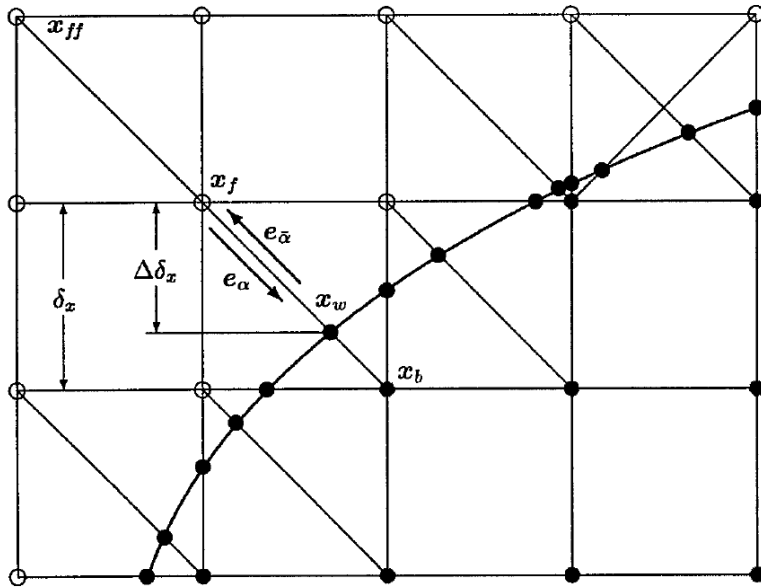


FIG. 2. Layout of the regularly spaced lattices and curved wall boundary. The thick curve marks the boundary location. The solid circles (●) mark the positions where particle-boundary collision occurs. The empty (○) and shaded (◐) circles are fluid sites and solid sides, respectively.

R. Mei, L-S Luo, and W. Shyy, NASA/CR-2000-209854, ICASE Report No. 2000-6

Bases of schemes:

1. Point-wise particle distribution interpolation
2. particle distribution transformation into local curve-linear coordinate system

Main drawback: mass conservation of fluid not insured.

— May not reliable/placticla for arbitrary moving boundaries

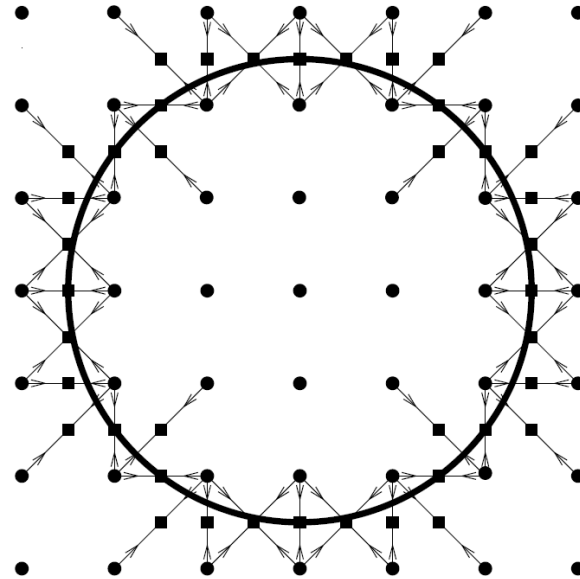


FIGURE 2. Location of the boundary nodes for a circular object of radius 2.5 lattice spacings. The velocities along links cutting the boundary surface are indicated by arrows. The location of the boundary nodes are shown by solid squares and the lattice nodes by solid circles.

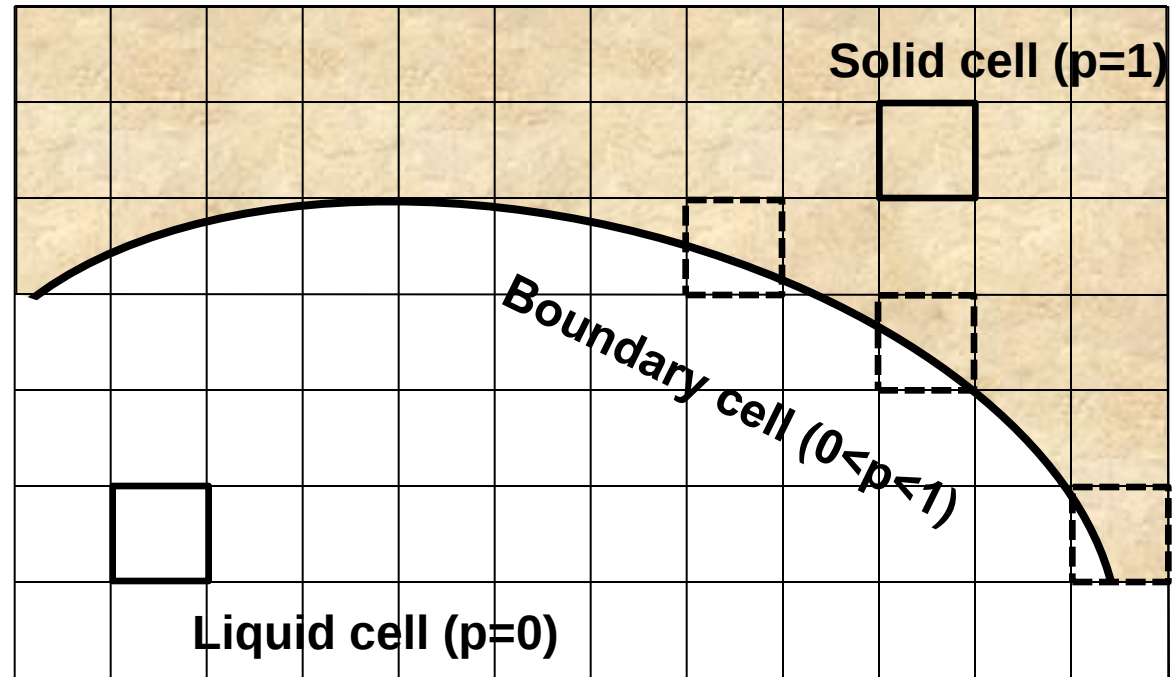
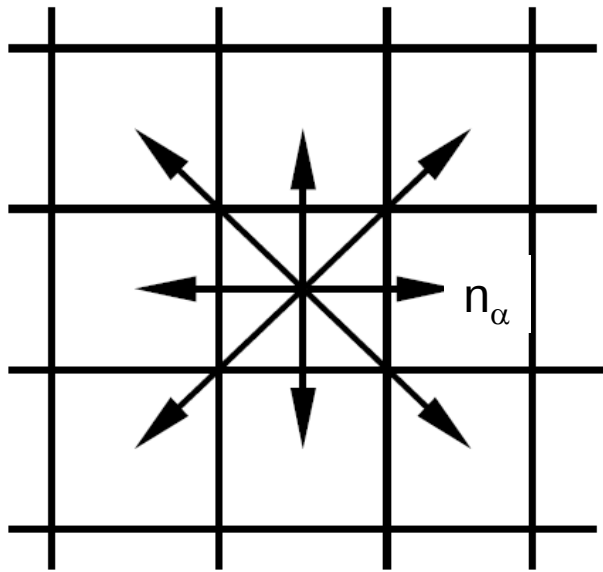
A. J. C. Ladd, JFM, 1994

Volumetric Representation

$$p(\vec{x}, t) = \frac{\Delta V_s(\vec{x}, t)}{\Delta V}$$

$$\Delta V = \Delta V_s + \Delta V_f$$

$$n_\alpha = f_\alpha \Delta V_f$$



When $\Delta V_s = 0$, $\Delta V_f = \Delta V$, volumetric representation recovers node-based description

Volumetric Lattice Boltzmann Equations

Time evolution of particle population

$$n_{\alpha}(\vec{x} + \vec{e}_{\alpha}\Delta t, t + \Delta t) = n_{\alpha}(\vec{x}, t) + \Omega_{\alpha}(\vec{x}, t)$$

$$\alpha = 0, 1, \dots, 8$$

$$N = \sum_{\alpha} n_{\alpha}$$

$$\vec{u}(\vec{x}, t) = \frac{\sum_{\alpha} \vec{e}_{\alpha} n_{\alpha}}{N}$$

$$\rho(\vec{x}, t) = \frac{N}{(1-p)\Delta V}$$

Particle population evolution consists of

- **Collision**

Momentum exchange between solid and fluid accounted

- **Streaming**

Volumetric bounce-back included

- **Boundary induced particle migration**

Mass conservation of fluid guaranteed

Collision

$$\Omega_{\alpha}(\vec{X}, t) = -\frac{1}{\tau} \left[n_{\alpha}(\vec{X}, t) - n_{\alpha}^{\text{eq}}(\vec{X}, t) \right] \quad \tau = \frac{1}{2} + \frac{3\nu}{c^2 \delta t}$$

$$n_{\alpha}^{\text{eq}}(\vec{X}, t) = N w_{\alpha} \left[1 + \frac{3(\vec{e}_{\alpha} \cdot \vec{U})}{2c^2} + \frac{9(\vec{e}_{\alpha} \cdot \vec{U})^2}{2c^4} - \frac{3U^2}{2c^2} \right] \quad \vec{U} = \vec{u} + \delta \vec{u}$$

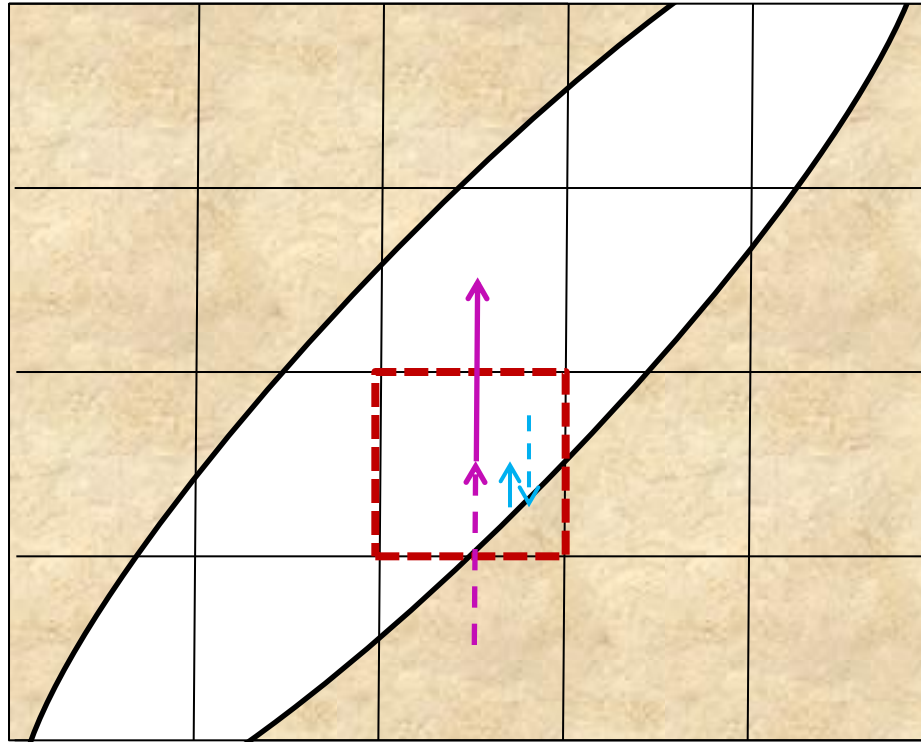
$$\delta \vec{u}(\vec{X}, t) = \tau p(\vec{X}, t) \vec{u}_b(\vec{X}, t) + \frac{\tau}{N(\vec{X}, t)} \sum_{\beta=1}^8 p(\vec{X} + \vec{e}_{\beta}, t) n_{\beta}(\vec{X}, t) \vec{u}_b(\vec{X} + \vec{e}_{\beta}, t)$$

1. Reflecting momentum change due to boundary movement ($\vec{u}_b \neq 0$)
2. Only for boundary cells and their neighboring fluid cells
3. Satisfying mass conservation in boundary cells

Streaming

(Generalized bounce-back condition)

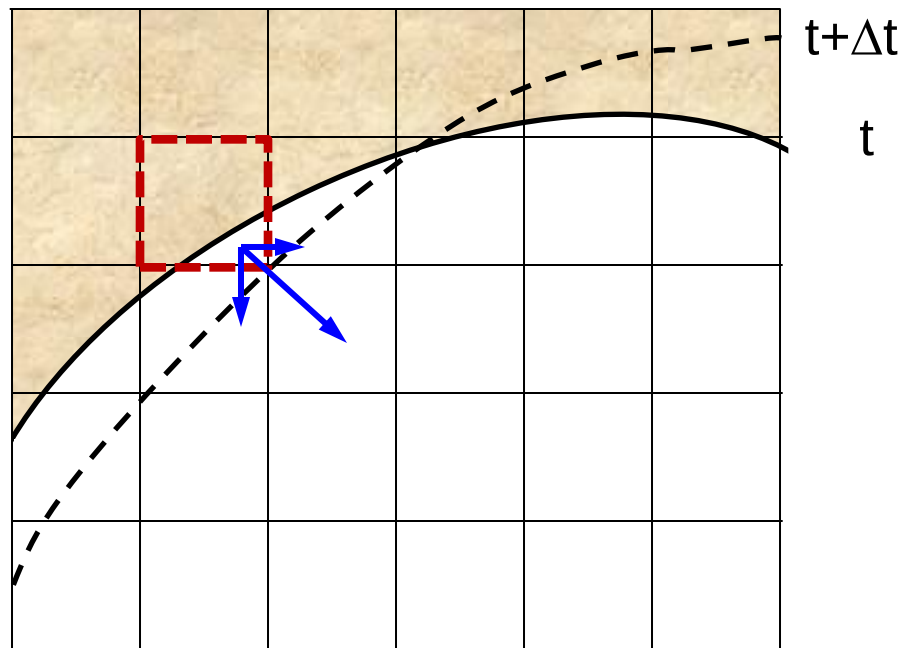
$$n''_{\alpha}(\vec{x}, t + \Delta t) = [1 - p(\vec{x}, t + \Delta t)] n'_{\alpha}(\vec{x} - \vec{e}_{\alpha} \Delta t, t) \leftarrow \text{Upwind streaming}$$
$$+ p(\vec{x} + \vec{e}_{\alpha^*}, t + \Delta t) n'_{\alpha^*}(\vec{x}, t) \leftarrow \text{Downwind bounce-back}$$



Boundary-induced Particle Migration

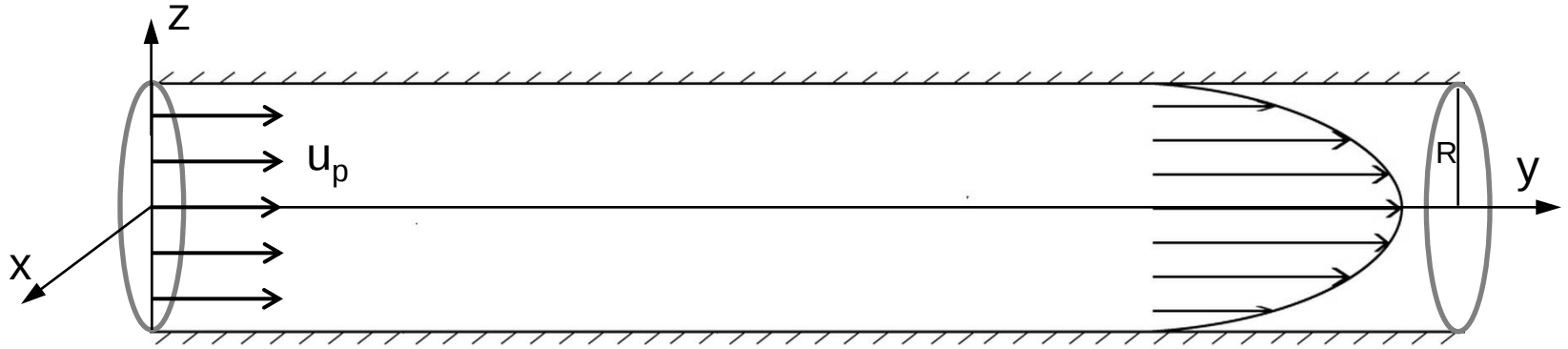
(mass conservation)

$$n_{\alpha}(\vec{x}, t + \Delta t) = [1 - p(\vec{x}, t + \Delta t)] n''_{\alpha}(\vec{x}, t + \Delta t) + \sum_{\beta=1}^b \tilde{n}_{\alpha,\beta}(\vec{x} - \vec{e}_{\alpha} \Delta t, t + \Delta t)$$



$$\tilde{n}_{\alpha,\beta}(\vec{x}, t + \Delta t) = p(\vec{x}, t + \Delta t) n''_{\alpha}(\vec{x}, t + \Delta t) \frac{[1 - p(\vec{x} + \vec{e}_{\beta} \Delta t, t + \Delta t)] n_{\beta}(\vec{x}, t)}{\sum_{k=1}^8 [1 - p(\vec{x} + \vec{e}_k \Delta t, t + \Delta t)] n_k(\vec{x}, t)}$$

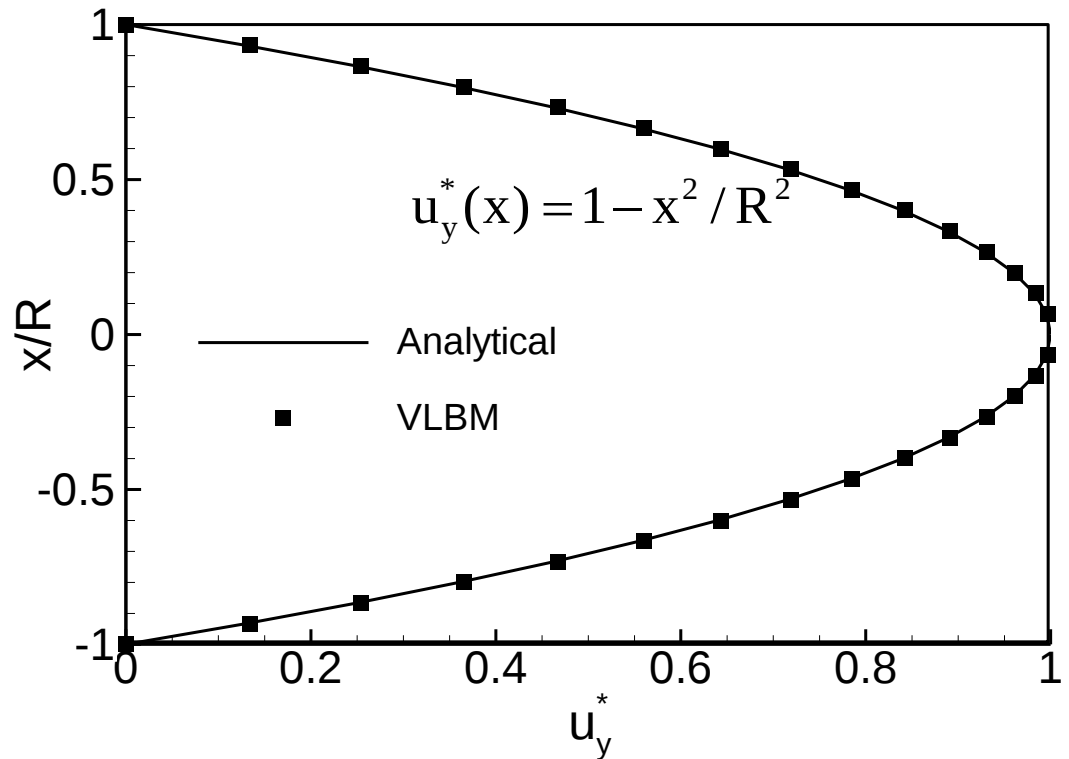
Steady Pipe Flow



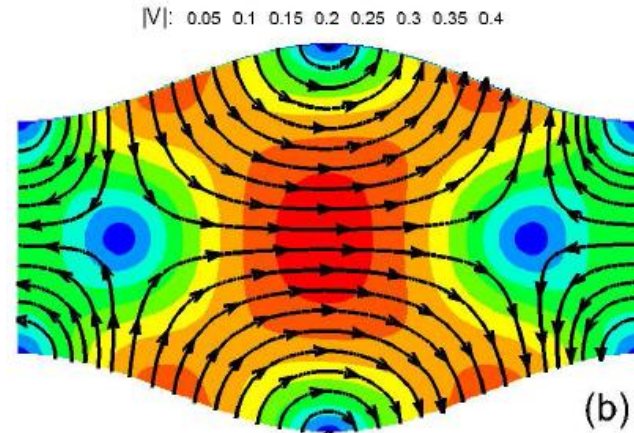
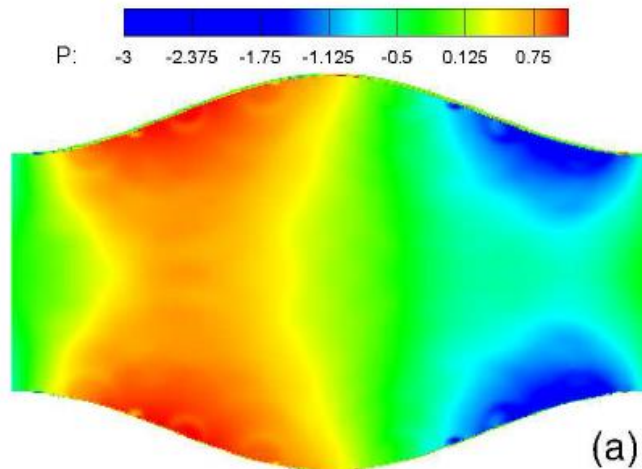
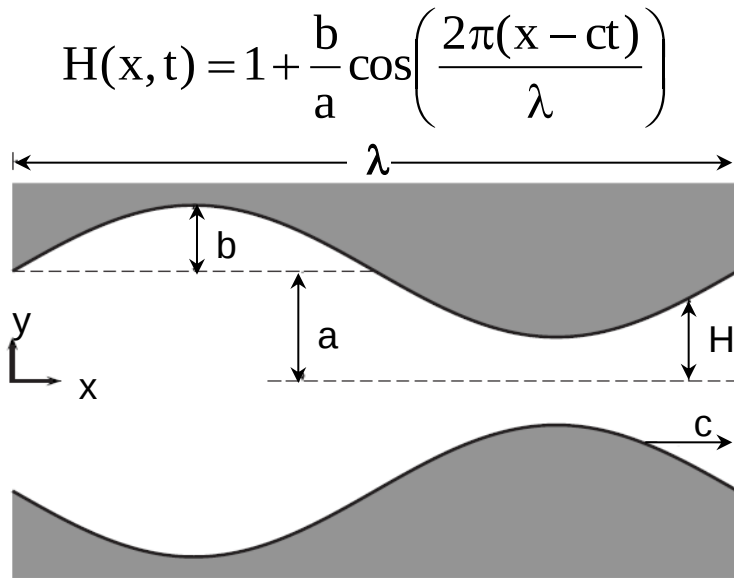
$$\frac{\partial^2 u_y}{\partial x^2} + \frac{\partial^2 u_y}{\partial z^2} = -\frac{1}{\mu} \frac{dp}{dy}$$

$$u_y(x, z) = 2u_p \left(1 - \frac{x^2 + z^2}{R^2} \right)$$

$$u_p = \frac{1}{8R^2} \left(\frac{1}{\mu} \frac{dp}{dy} \right)$$

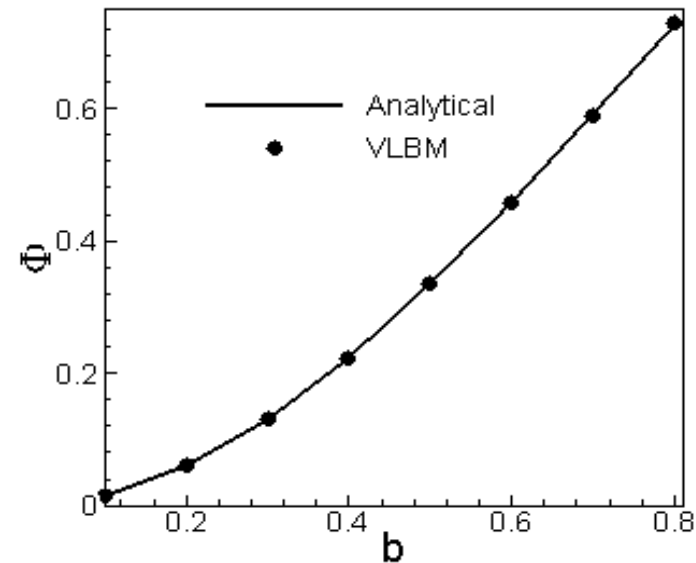


Peristaltic Flow



$$\Phi = \frac{Q}{ac} = \frac{3b^2}{2a^2 + b^2}$$

Shapiro, Jaffrin, and Weinberg, JFM 1969
Jaffrin and Shapiro, Annu Rev Fluid Mech 1971



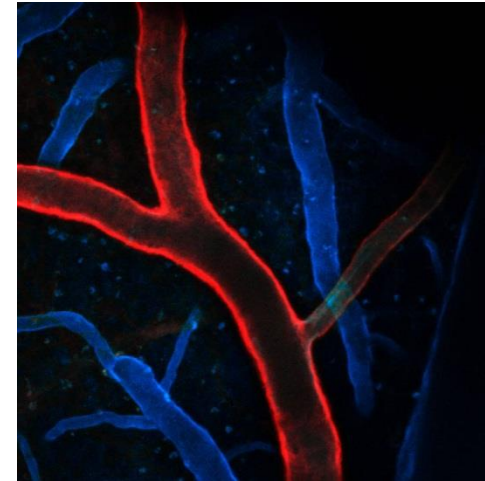
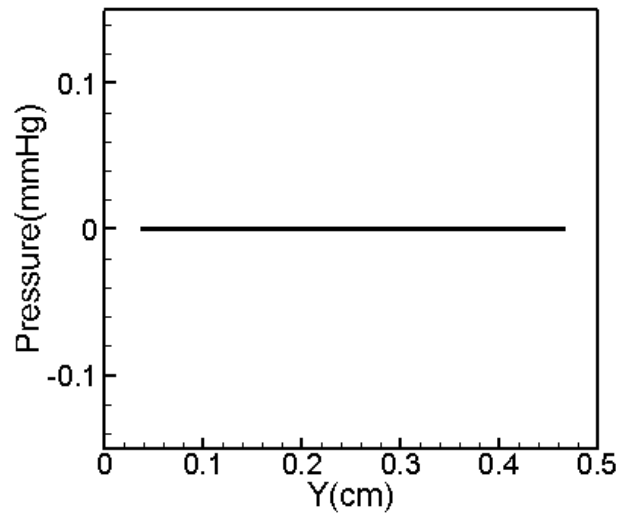
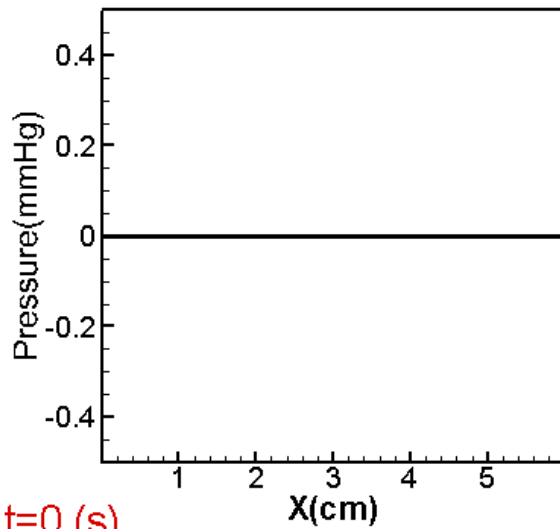
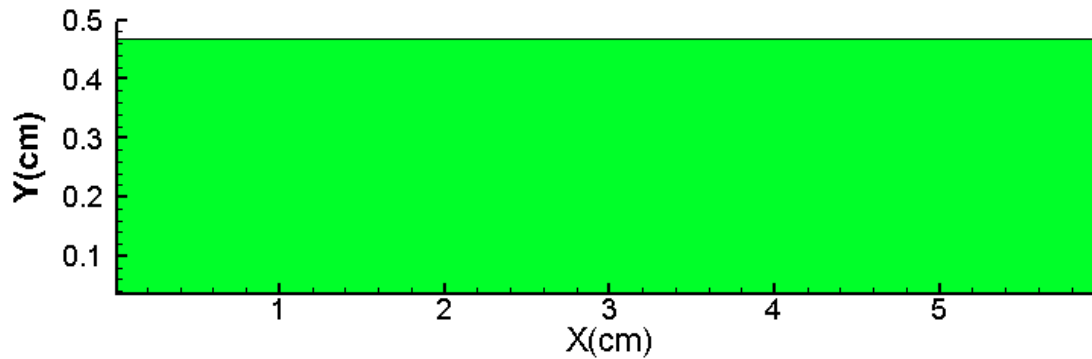
$$\frac{a}{\lambda} = \frac{\pi}{80}, \quad \text{Re} = \frac{2ac}{\nu} = 4$$

Artery Wall Motility

Artery walls in the brain



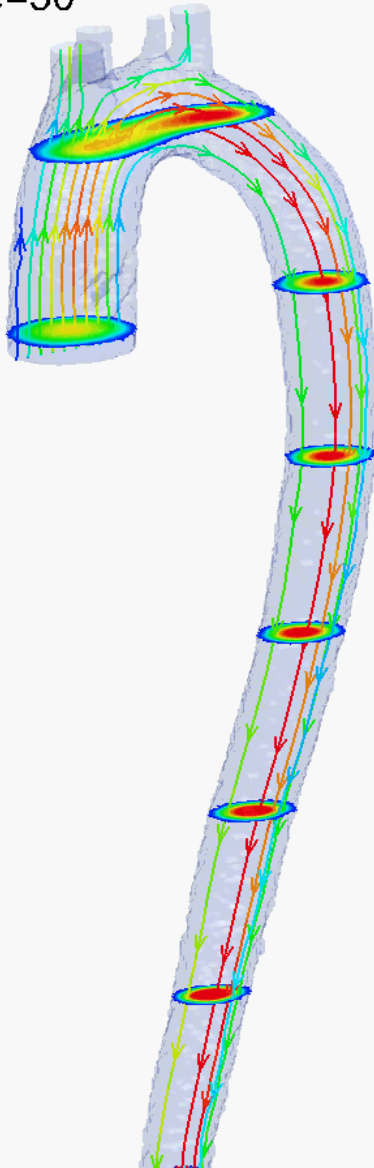
Pressure(mmHg): -0.1 -0.08 -0.06 -0.04 -0.02 0 0.02 0.04 0.06 0.08 0.1



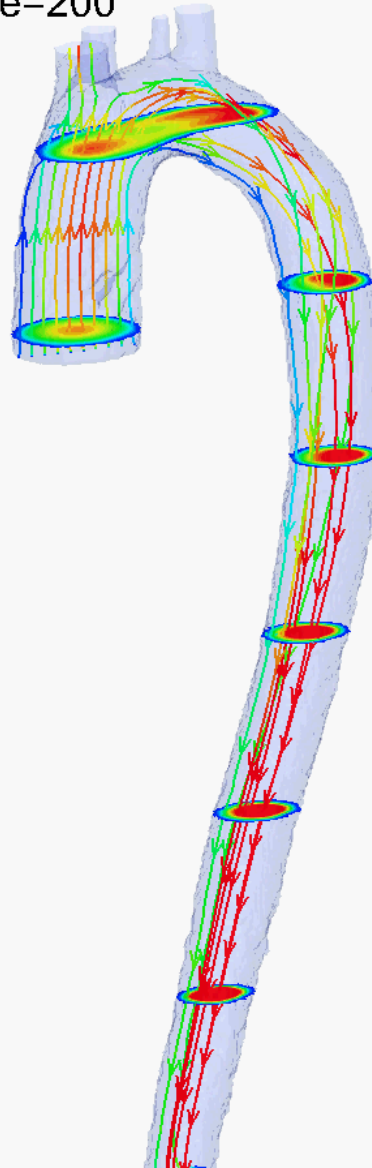
Preliminary Results of Hemodynamics in Healthy and Diseased Aortas

Healthy, Streamlines

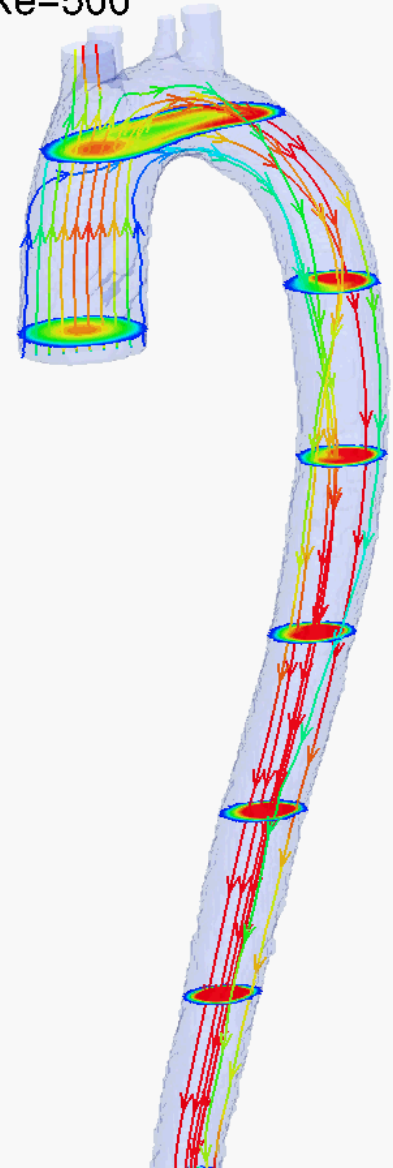
Re=50



Re=200

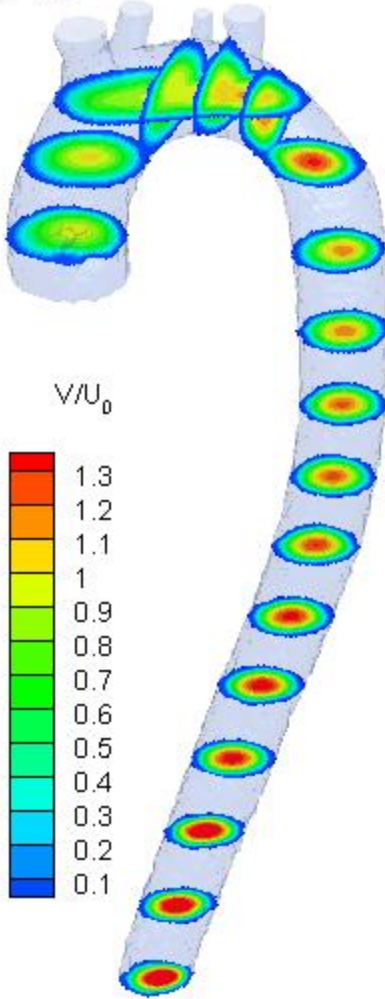


Re=500

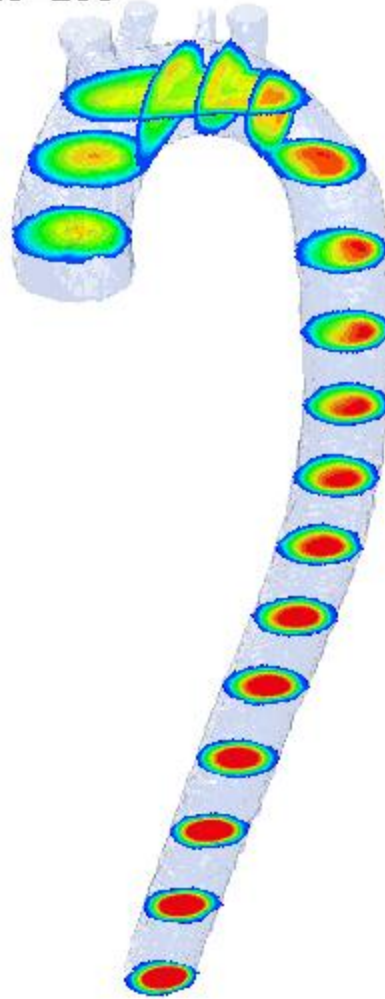


Healthy Velocity

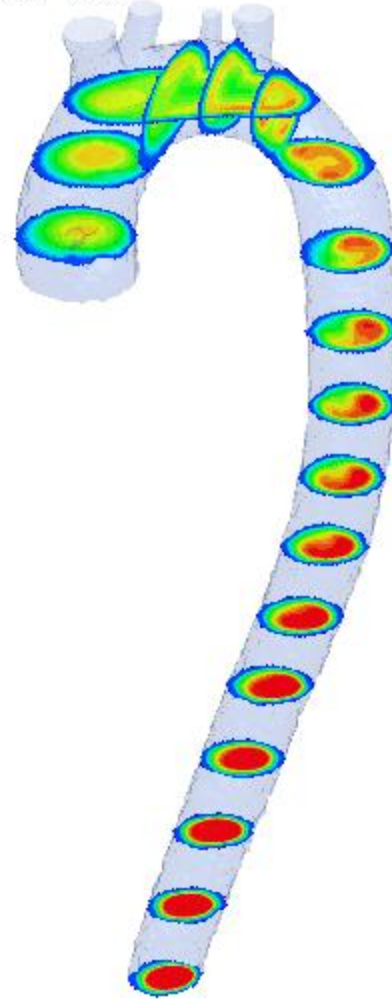
Re=50



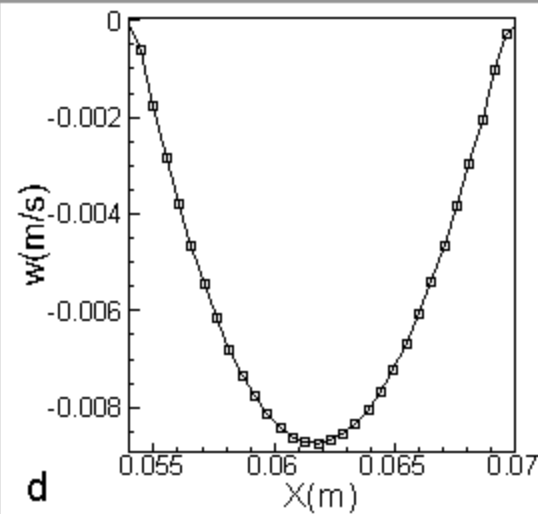
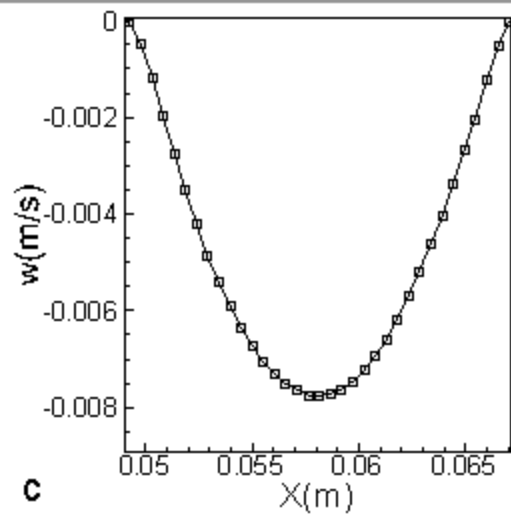
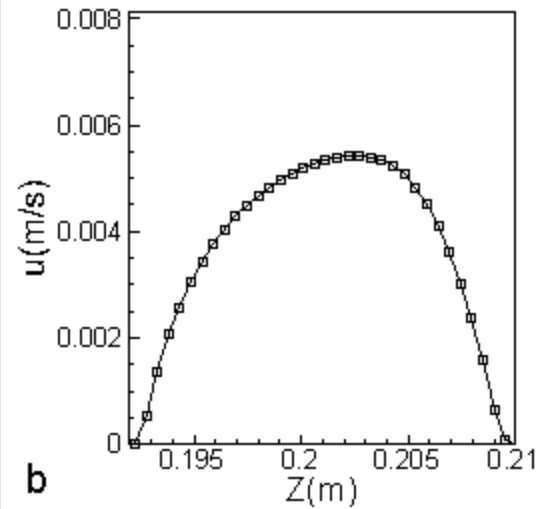
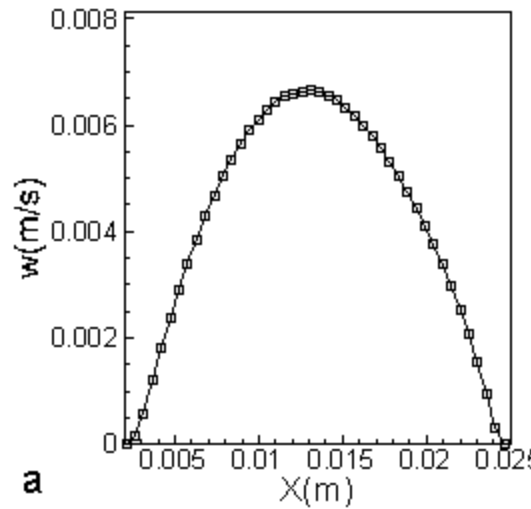
Re=200



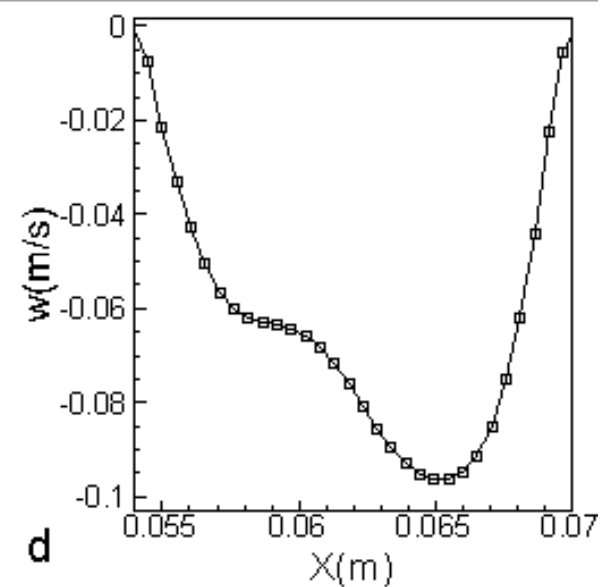
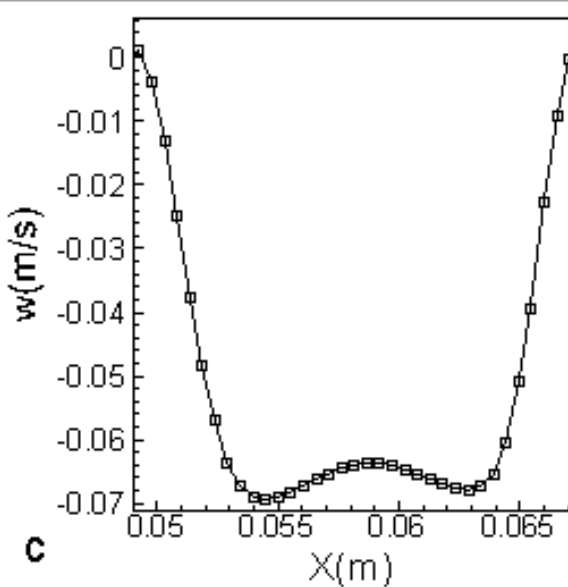
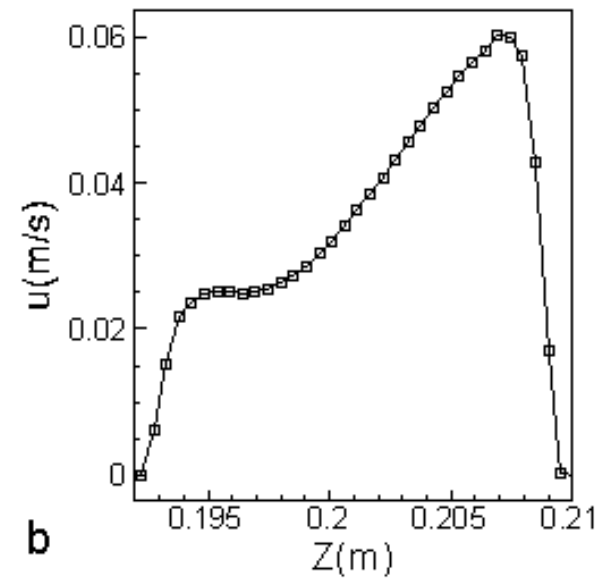
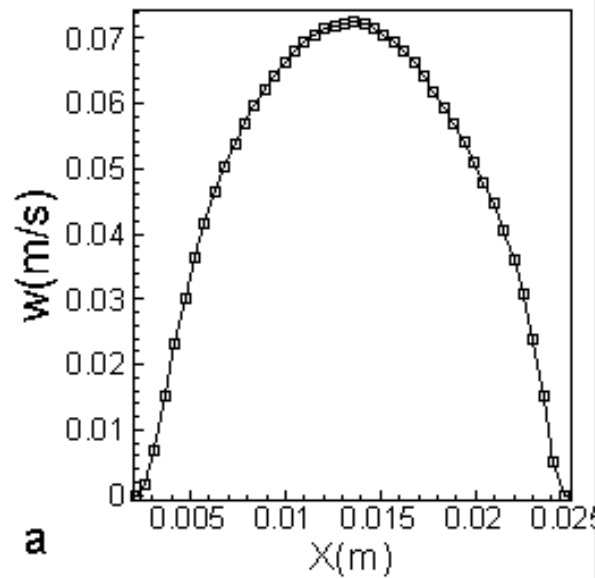
Re=500



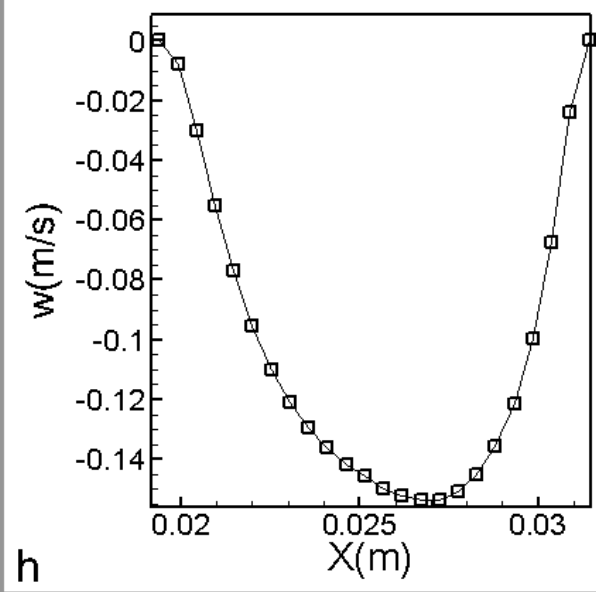
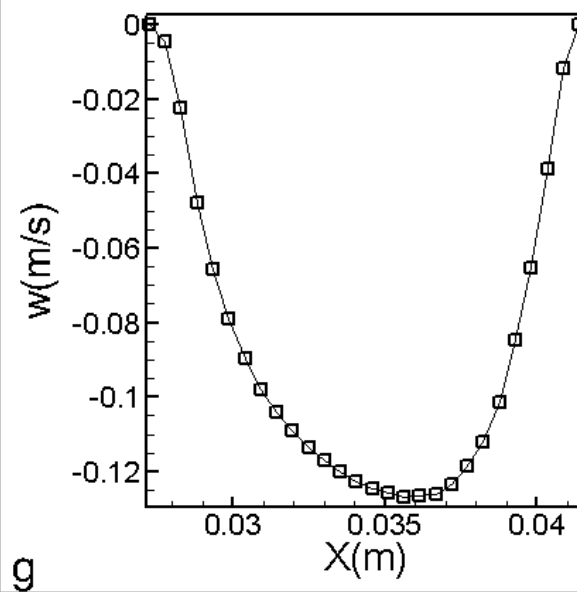
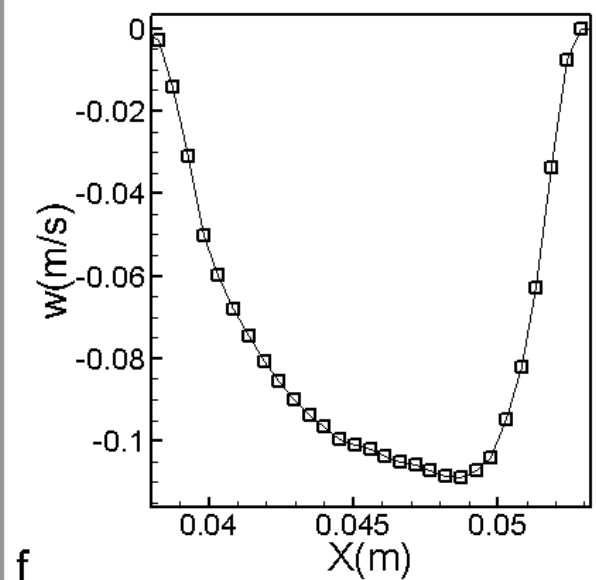
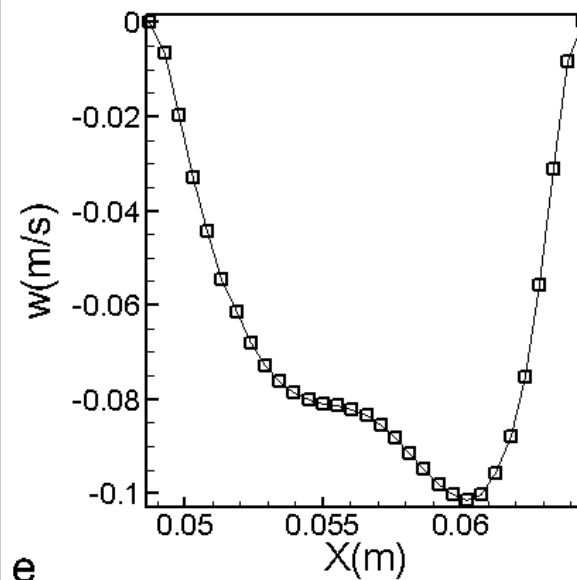
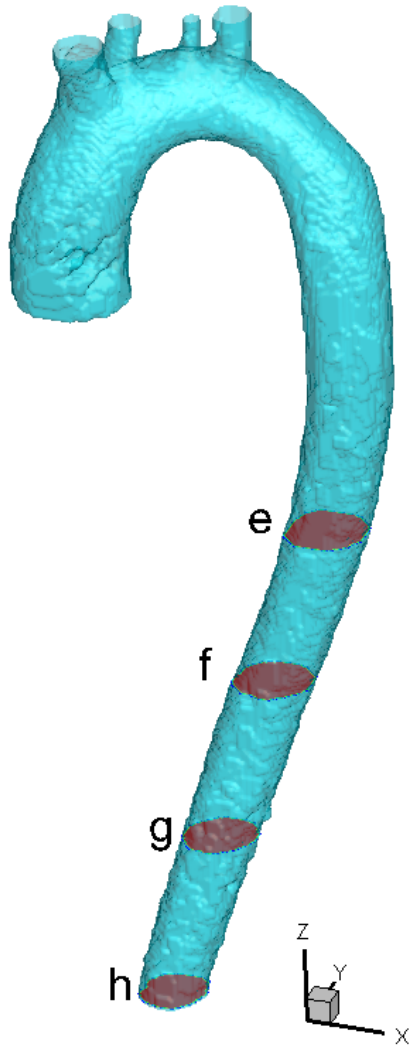
Healthy Velocity , $Re=50$



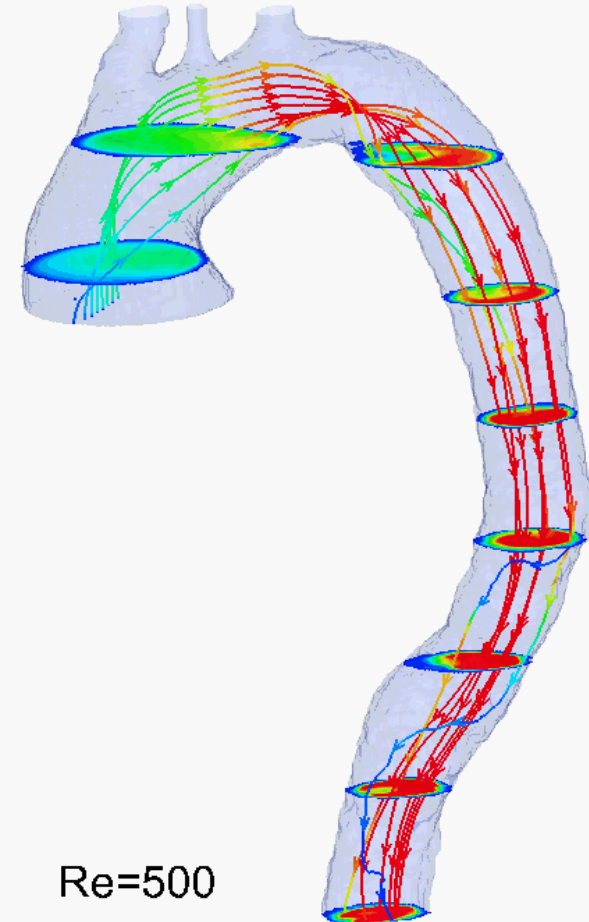
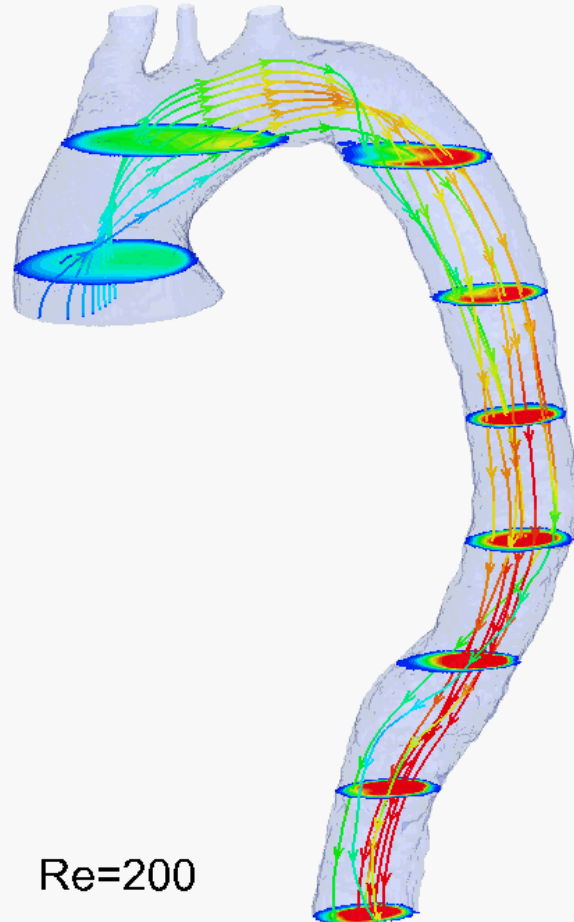
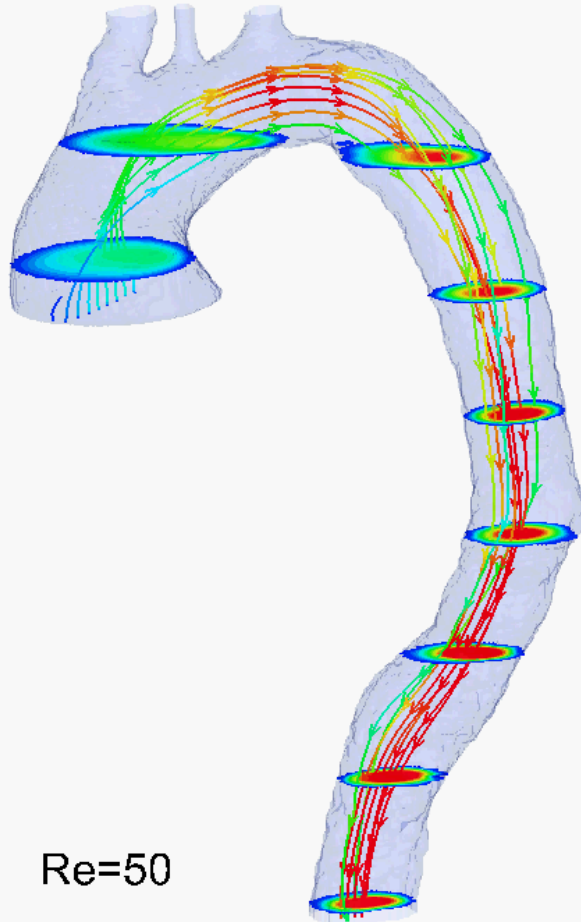
Healthy Velocity, $Re=500$



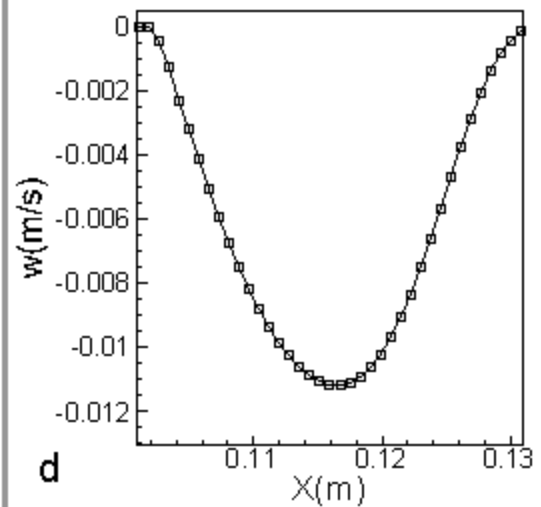
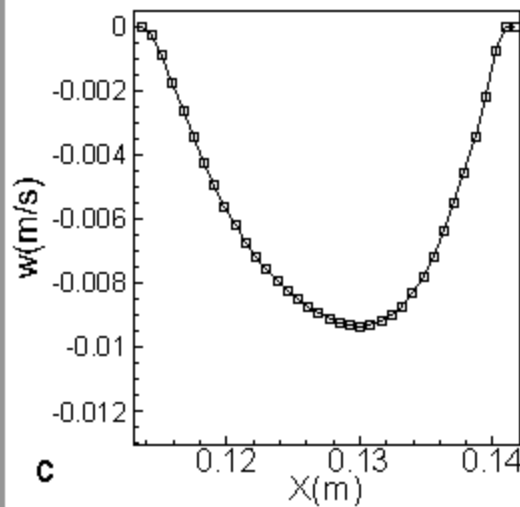
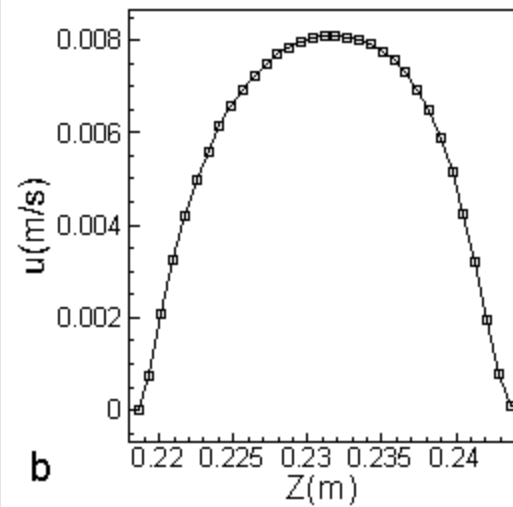
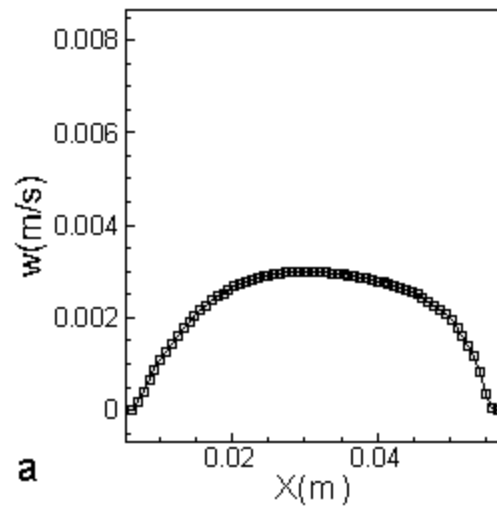
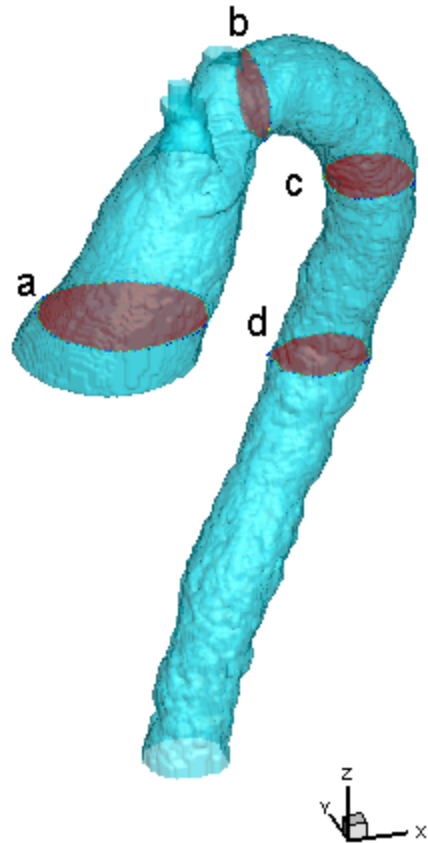
Healthy Velocity, $Re=500$, cont'd



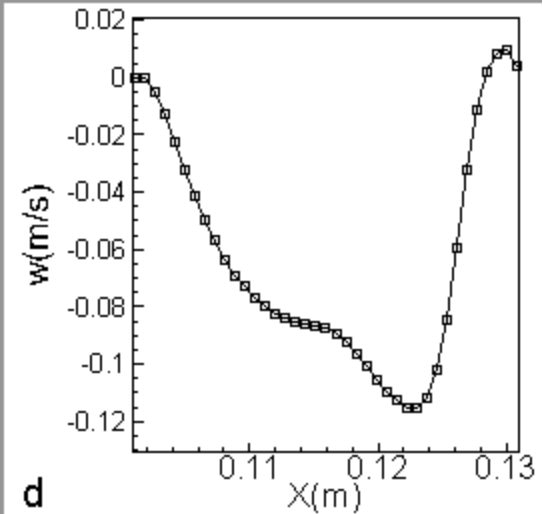
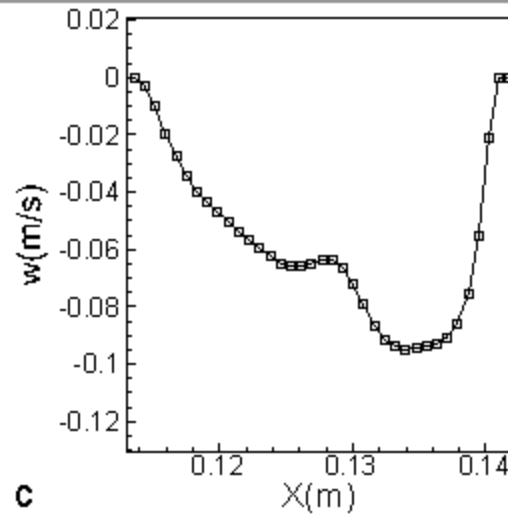
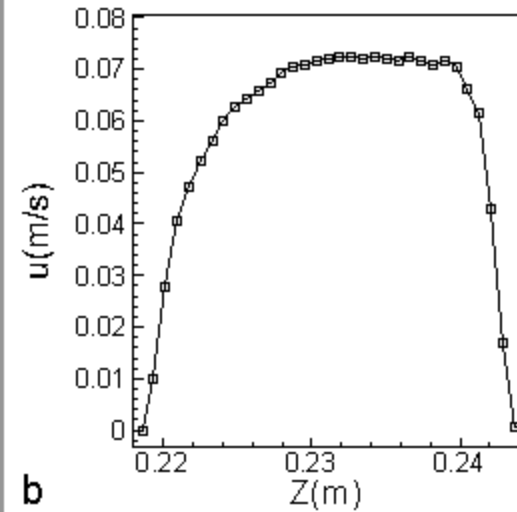
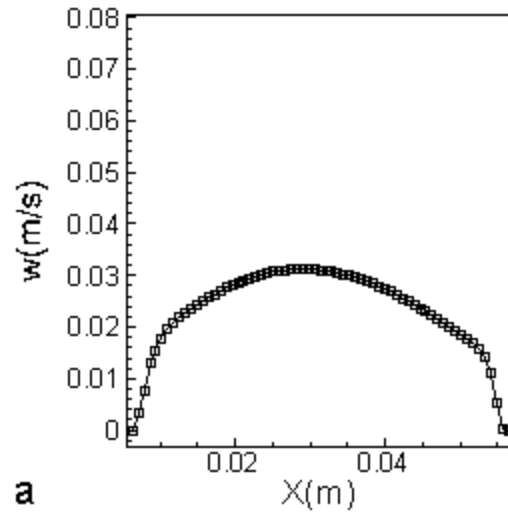
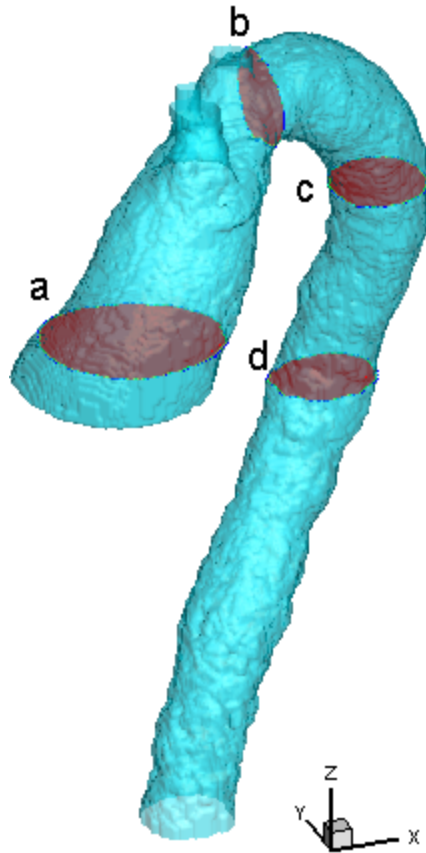
Dilated, Streamlines



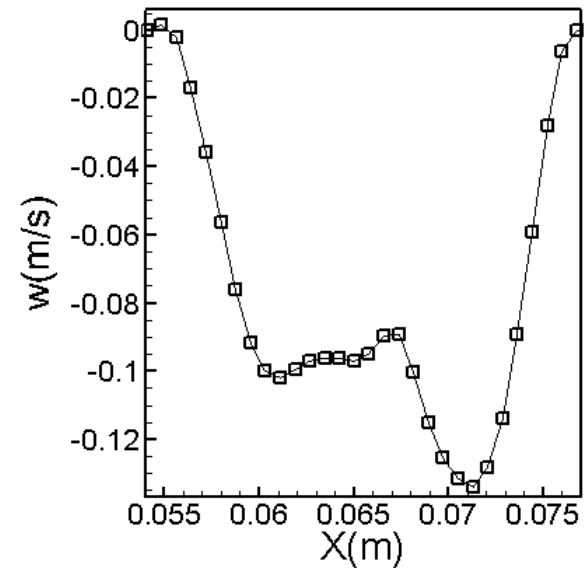
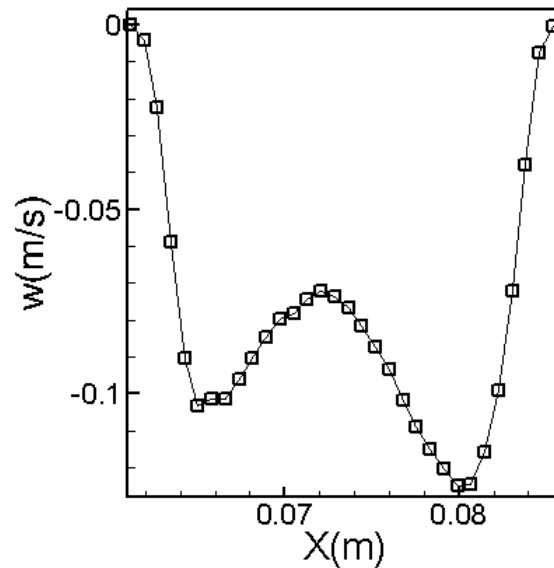
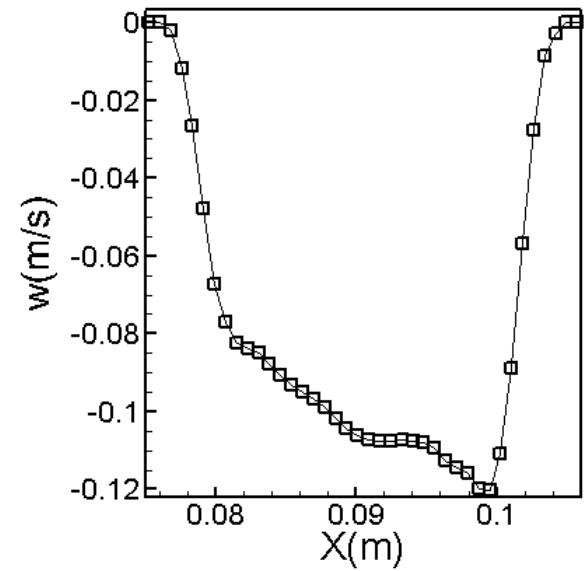
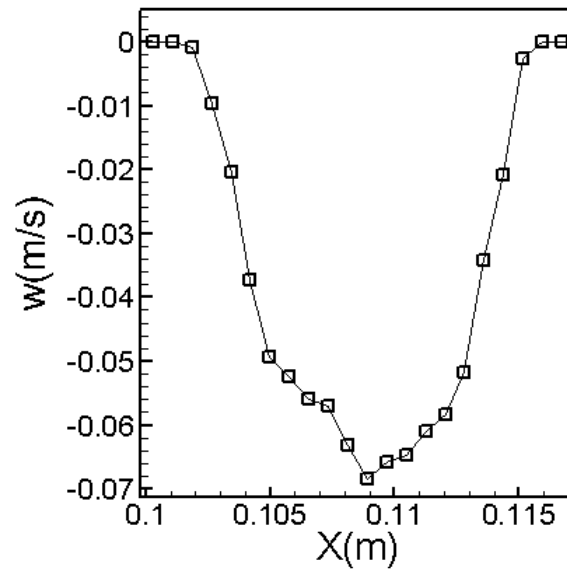
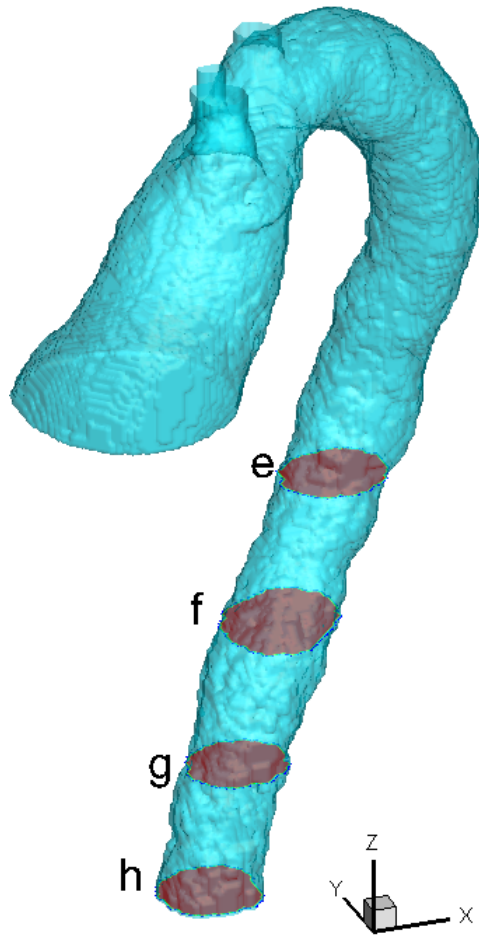
Dilated Velocity, $Re=50$



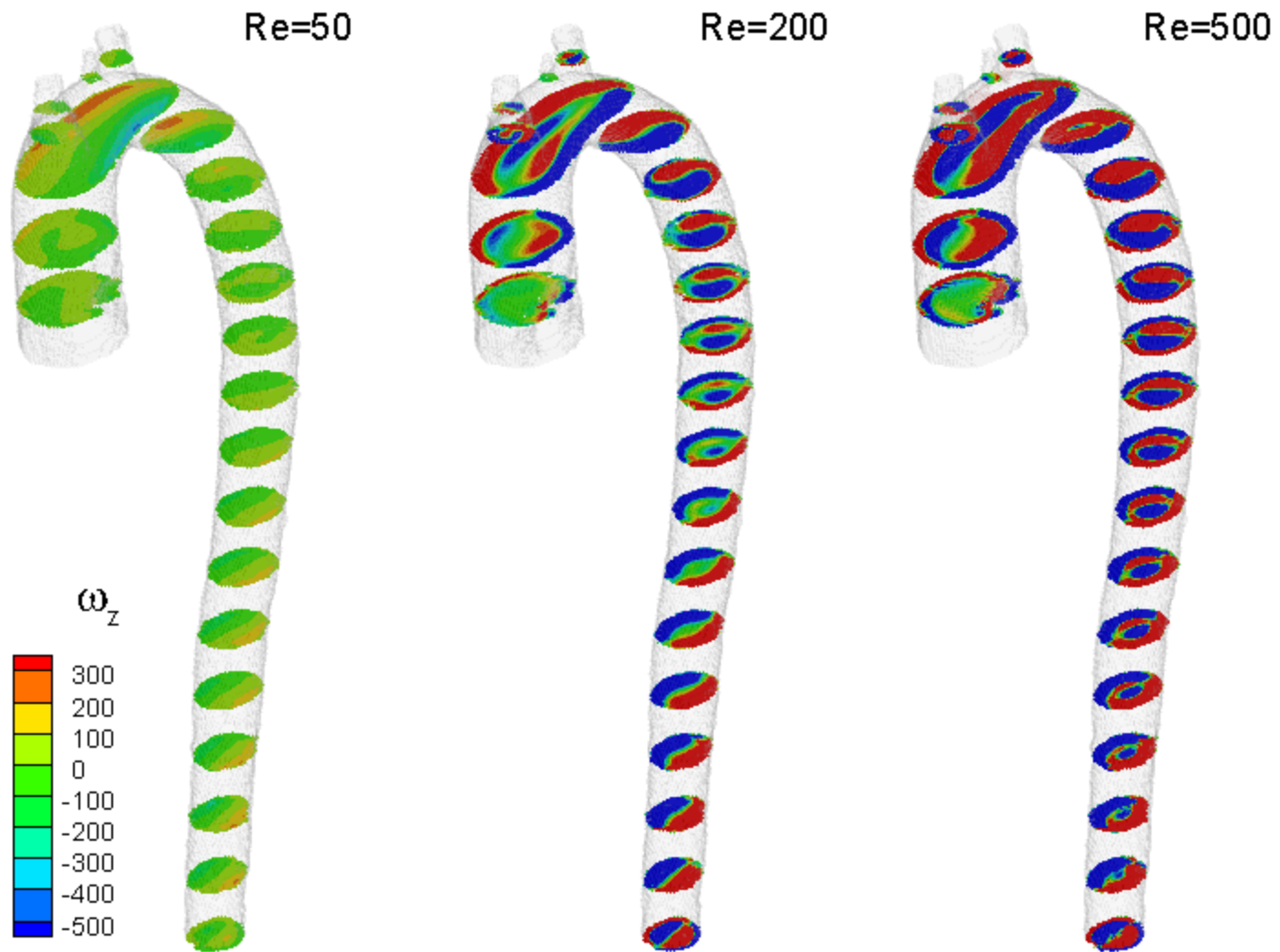
Dilated Velocity, $Re=500$



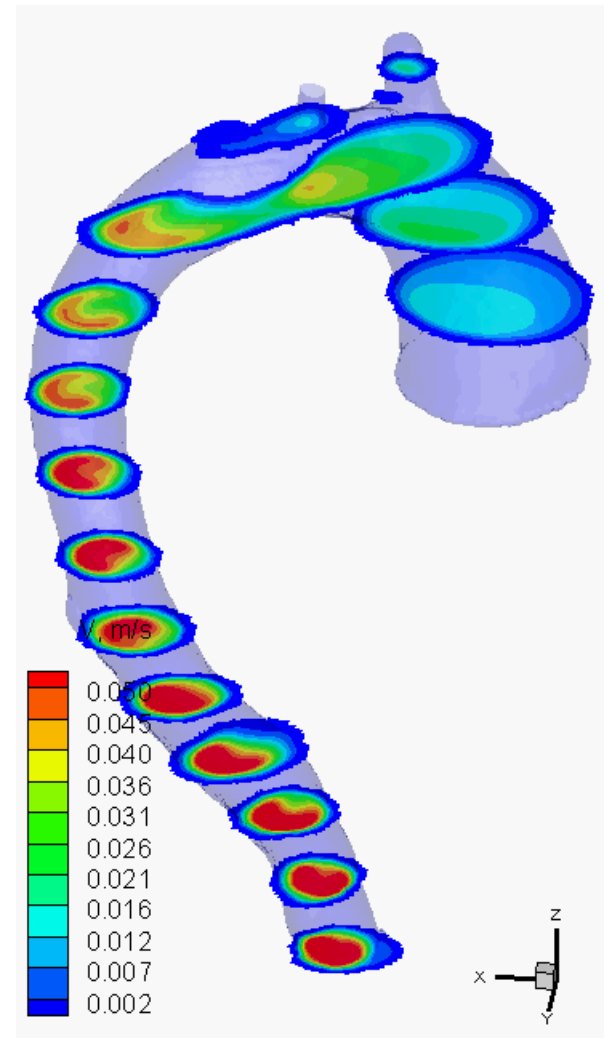
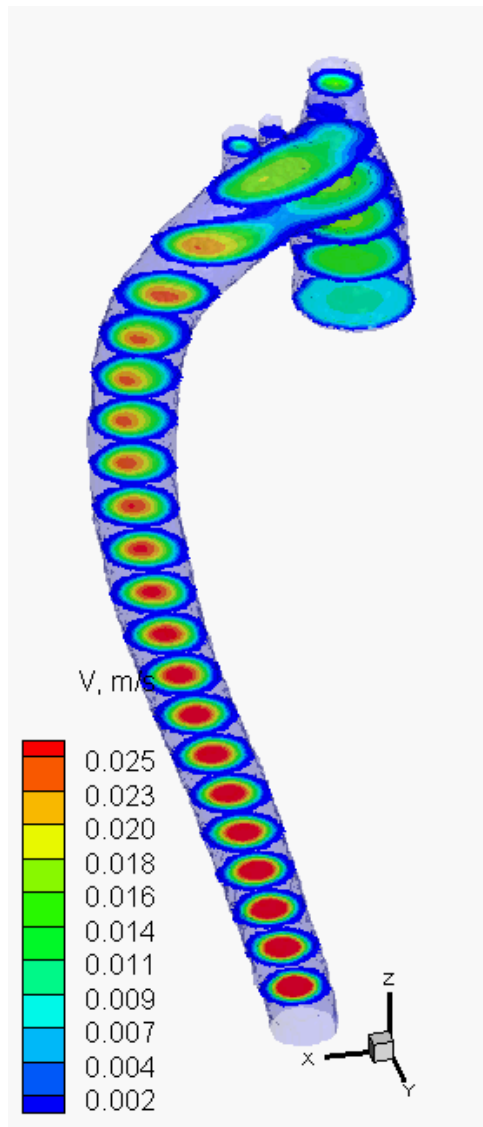
Dilated Velocity, $Re=500$, cont'd



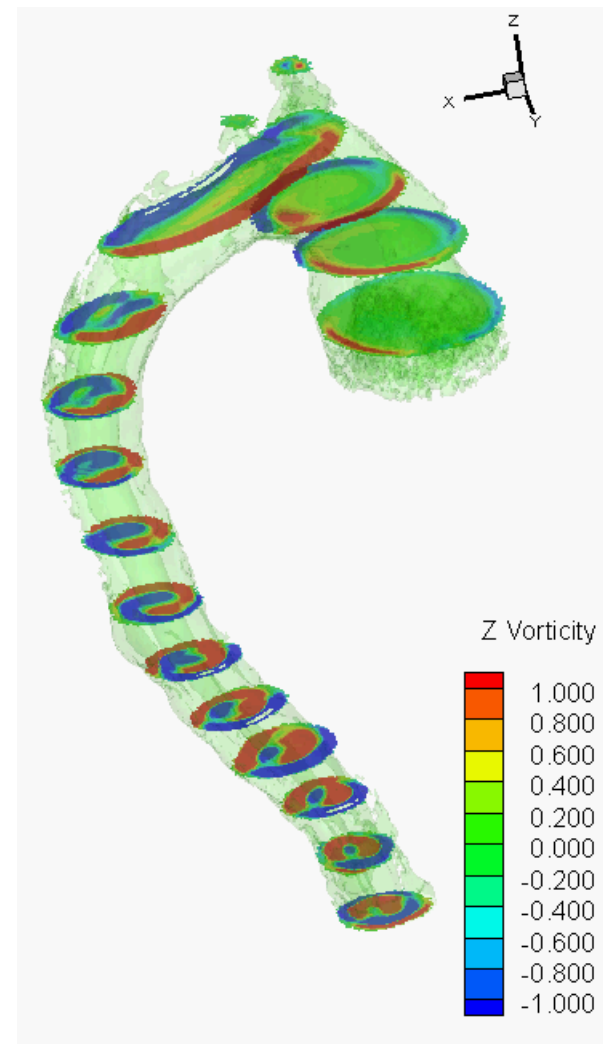
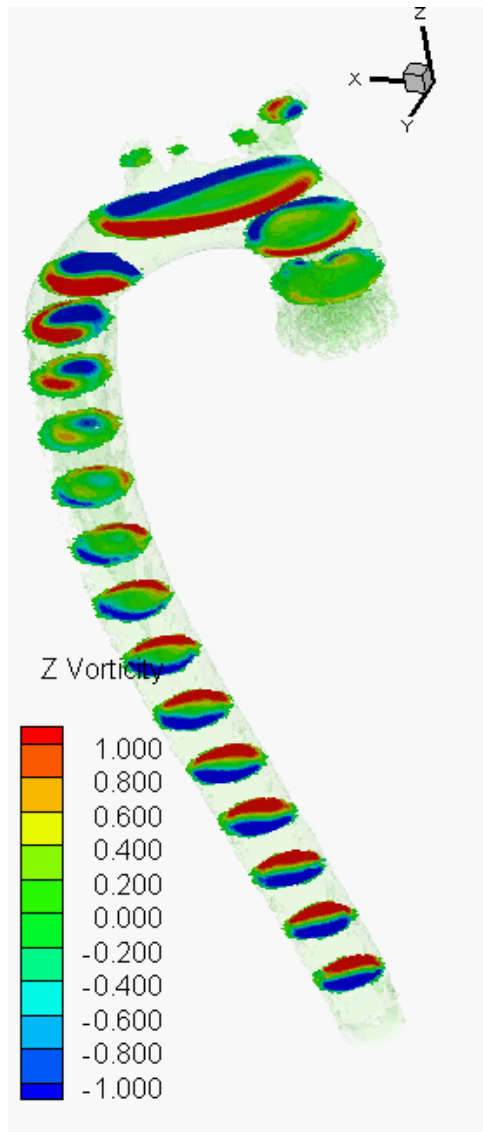
Healthy, Vorticity



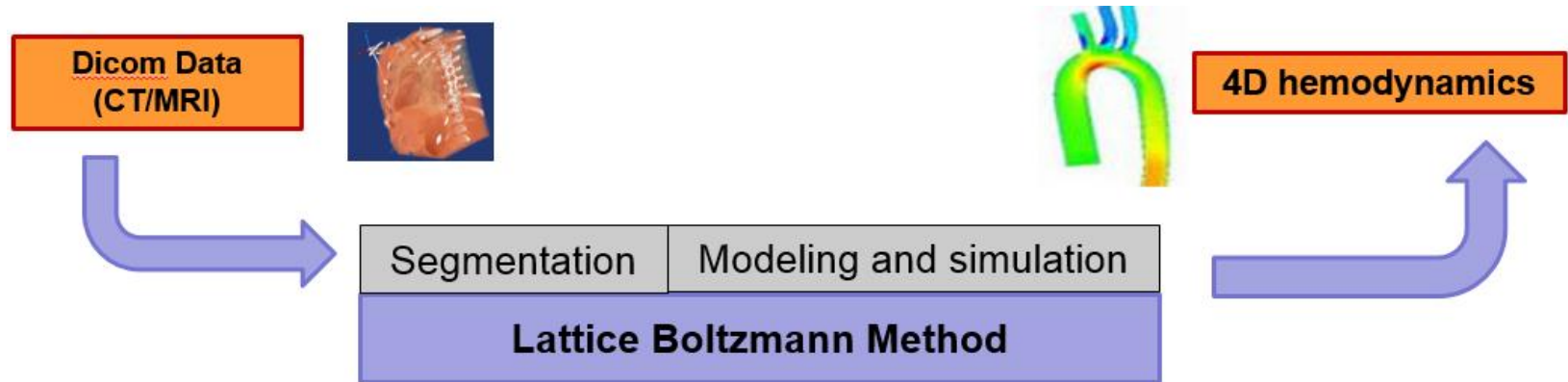
Healthy vs. Dialted, Velocity



Healthy vs. Dilated Vorticity



Take-Home Messages



Unified computation platform

1. Good for patient-specific flows in human organs
Cardiovascular blood flow in coronary, aorta, carotid --- heart attack, stroke
Peristalsis in stomach, esophagus, urine --- cancers
2. Pulsatility --- Laminar, transitional, turbulence
3. Non-Newtonian --- multiphase
4. GPU parallel computation

Medical focus

1. Patient-specific hemodynamics in carotid artery --- Hemodynamic indicators to distinguish symptomatic and asymptomatic carotid stenosis to stroke
2. Supplemental device to CT/MRI to reveal real-time hemodynamics in diseased human organs.